

Correspondence

Novel Partial Selection Schemes for AF Relaying in Nakagami- m Fading Channels

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Abstract—New partial relay selection schemes for cooperative diversity based on amplify-and-forward (AF) relaying are proposed in Nakagami- m fading channels. Their performances are compared with the conventional partial selection scheme. Numerical results show that the new schemes have performance gains of up to 5 dB over the conventional scheme. In some cases, their performances are indistinguishable from the full selection scheme, but they have much simpler structures. Numerical results also show that it is more important to choose the idle user for the hop with a small average signal-to-noise ratio (SNR) or an m parameter in partial selection. Based on this observation, a new adaptive partial selection scheme based on the average SNR, and the m parameter is derived. A complexity analysis also shows that the new schemes reduce the complexity in some cases.

Index Terms—Amplify-and-forward (AF), performance analysis, user selection.

I. INTRODUCTION

In recent years, cooperative diversity has been proposed as an effective method of improving the performance of a wireless system [1]. In a cooperative diversity system, idle users are employed to forward signals from the source to the destination. The idle users act as virtual antennas to achieve cooperative space diversity at the destination, in contrast to the traditional diversity system where multiple antennas are physically installed at the destination [2]–[5]. Among all the existing protocols for cooperative diversity, amplify-and-forward

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(AF) relaying is one of the simplest protocols [1]. The performance of AF cooperative diversity improves as the number of idle users increases [6]. However, the complexity of the network also increases as the number of the idle users increases. In some applications, such as wireless sensor networks, complexity is more important than performance in the performance–complexity design tradeoff for wireless systems to achieve long battery life once the minimum performance requirement is met. To reduce the network complexity in these applications, user selection is implemented that often chooses one out of all available idle users for AF cooperative diversity.

In [7], the optimal full selection scheme was proposed by choosing the idle user with the largest instantaneous end-to-end signal-to-noise ratio (SNR). In [8] and [9], two suboptimal full selection schemes were proposed by choosing the idle user with the largest harmonic mean or the minimum of the instantaneous SNRs of the first and second hops. In [10], a subset of idle users was chosen by comparing their combined instantaneous SNR with a preset threshold. In [11], time-varying channels were considered for relay selection. All these selection schemes require knowledge of the instantaneous SNRs of both the first and second hops for each idle user. To reduce complexity, [12] proposed a partial selection scheme that only compares the instantaneous SNR of the first hop for each idle user in Rayleigh fading channels. In [13] and [14], the scheme proposed in [12] was evaluated by considering the feedback delay and multiple antennas at the destination, respectively.

In this paper, we propose three new partial selection schemes for AF cooperative diversity with variable relay gain. The exact expression for the error rate of the first new scheme is analytically derived, whereas the error rates of the second and third new schemes are calculated via simulations. Moreover, we derive the exact expressions for the error rates of the optimal full selection scheme and the conventional partial selection scheme for Nakagami- m fading channels. To the best of the authors’ knowledge, these are not available in the literature. Numerical results show that the new partial selection schemes have performance gains of up to 5 dB over the conventional partial selection scheme, and in some cases, their performances are very close to that of the optimal full selection scheme, but they have much simpler structures. It is also shown that choosing the best idle user for the hop with a smaller average SNR or an m parameter is important. Based on this, we also propose a new adaptive partial selection scheme by using the average SNR and the Nakagami m parameter, which can be estimated using results in [15].

II. RELAY SELECTION

Similar to [12], consider an AF cooperative diversity system with one source, one destination, and N relays. There is no direct link between the source and the destination. The idle user links have two-hop transmissions. In the first time slot, the source transmits the signal to the idle users such that the received signal at the k th idle user can be expressed as

$$u_k(t) = h_{1,k} \sqrt{E_1} x(t) + n_{1,k}(t) \quad (1)$$

where $k = 1, 2, \dots, N$ is the user index, $h_{1,k}$ is the complex fading gain in the channel between the source and the k th idle user, E_1 is the transmitted signal energy, $x(t)$ is the transmitted signal, and $n_{1,k}(t)$ is the complex Gaussian noise in the channel between the source and

83 the k th idle user with noise power $N_{1,k}$. In the second time slot, the
84 received signals at the idle users are amplified and transmitted such
85 that the received signal from the k th idle user at the destination is

$$y_k(t) = h_{2,k}\alpha_k u_k(t) + n_{2,k}(t) \quad (2)$$

86 where $h_{2,k}$ is the complex fading gain in the channel between the k th
87 idle user and the destination, $\alpha_k = \sqrt{E_{2,k}/(E_1|h_{1,k}|^2 + N_{1,k})}$ is the
88 amplification factor, $E_{2,k}$ is the radiated energy at the k th idle user,
89 and $n_{2,k}(t)$ is the complex Gaussian noise in the channel between the
90 k th idle user and the destination with noise power $N_{2,k}$. All the links
91 experience Nakagami- m fading such that $|h_{1,k}|$ follows a Nakagami
92 distribution with $E\{|h_{1,k}|^2\} = \Omega_{1,k}$ and m parameter $m_{1,k}$, whereas
93 $|h_{2,k}|$ follows a Nakagami distribution with $E\{|h_{2,k}|^2\} = \Omega_{2,k}$ and
94 m parameter $m_{2,k}$. In this paper, it is assumed that $E_{2,k} = E_2$,
95 $N_{1,k} = N_1$, $N_{2,k} = N_2$, $\Omega_{1,k} = \Omega_1$, $\Omega_{2,k} = \Omega_2$, $m_{1,k} = m_1$, and
96 $m_{2,k} = m_2$ for $k = 1, 2, \dots, N$, similar to [12]. The instantaneous
97 end-to-end SNR of the k th link can be shown as $\gamma_k = \gamma_{1,k}\gamma_{2,k}/\gamma_{1,k} +$
98 $\gamma_{2,k} + 1$, where $\gamma_{1,k} = |h_{1,k}|^2 E_1/N_1$ and $\gamma_{2,k} = |h_{2,k}|^2 E_2/N_2$ are
99 the instantaneous SNRs of the first and second hops, respectively. In
100 Nakagami- m fading channels, $\gamma_{1,k}$ follows a Gamma distribution with
101 shape parameter m_1 and scale parameter $\bar{\gamma}_1/m_1$, whereas $\gamma_{2,k}$ follows
102 a Gamma distribution with shape parameter m_2 and scale parameter
103 $\bar{\gamma}_2/m_2$, where $\bar{\gamma}_1 = \Omega_1 E_1/N_1$ and $\bar{\gamma}_2 = \Omega_2 E_2/N_2$ are the average
104 SNRs of the first and second hops, respectively.

105 A. Optimal Full Selection Scheme

106 In the optimal full selection scheme, the idle user is selected
107 according to

$$K = \max_{k=1,2,\dots,N} \{\gamma_k\}. \quad (3)$$

108 Denote this scheme as the $\max\{\gamma_k\}$ scheme. Using (3), the error rate
109 can be derived as

$$P_e = \int_0^\infty P(e|x) f_{\gamma_K}(x) dx = \int_0^\infty P(e|x) dF_{\gamma_K}(x) \quad (4)$$

110 where $P(e|x)$ is the conditional probability of error, which is con-
111 ditioned on γ_K , and $f_{\gamma_K}(x)$ and $F_{\gamma_K}(x)$ are the probability den-
112 sity function (pdf) and the cumulative distribution function (cdf) of
113 $\gamma_K = \max\{\gamma_1, \gamma_2, \dots, \gamma_N\}$, respectively. Since $\gamma_1, \gamma_2, \dots, \gamma_N$ are
114 independent and identically distributed, one has $F_{\gamma_K}(x) = F_{\gamma_k}^N(x)$,
115 where $F_{\gamma_k}(x)$ is the cdf of γ_k given by [16, eq. (2)]

$$\begin{aligned} F_{\gamma_k}(x) &= 1 - \frac{2m_2^{m_2}(m_1-1)! e^{-\frac{m_1}{\bar{\gamma}_1}x - \frac{m_2}{\bar{\gamma}_2}x}}{\bar{\gamma}_2^{m_2}\Gamma(m_1)\Gamma(m_2)} \\ &\times \sum_{i_1=0}^{m_1-1} \sum_{i_2=0}^{i_1} \sum_{i_3=0}^{m_2-1} \frac{\binom{i_1}{i_2} \binom{m_2-1}{i_3}}{i_1!} \left(\frac{m_2}{\bar{\gamma}_2}\right)^{\frac{i_2-i_3-1}{2}} \\ &\cdot \left(\frac{m_1}{\bar{\gamma}_1}\right)^{\frac{2i_1-i_2+i_3+1}{2}} x^{\frac{2i_1+2m_2-i_2-i_3-1}{2}} \\ &\cdot (x+1)^{\frac{i_2+i_3+1}{2}} K_{i_2-i_3-1} \left(2\sqrt{\frac{m_1 m_2 x(1+x)}{\bar{\gamma}_1 \bar{\gamma}_2}}\right) \end{aligned} \quad (5)$$

116 with $K_{i_2-i_3-1}(\cdot)$ being the $(i_2 - i_3 - 1)$ th-order modified Bessel
117 function of the second kind [17, 8.432]. From (4), one has

$$P_e = \int_0^\infty P(e|x) dF_{\gamma_k}^N(x). \quad (6)$$

Using integration by parts, one further has

$$P_e = P(e|x) F_{\gamma_k}^N(x) \Big|_0^\infty - \int_0^\infty F_{\gamma_k}^N(x) dP(e|x). \quad (7)$$

For binary phase-shift keying (BPSK), one has $P(e|x) = Q(\sqrt{2x})$,
where $Q(\cdot)$ is the Gaussian- Q function, which is defined as $Q(x) =$
 $(1/\sqrt{2\pi}) \int_x^\infty e^{-(t^2/2)} dt$, giving

$$P_e = \frac{1}{\sqrt{4\pi}} \int_0^\infty F_{\gamma_k}^N(x) \frac{e^{-x}}{\sqrt{x}} dx \quad (8)$$

because $Q(\sqrt{2x}) F_{\gamma_k}^N(x) \Big|_0^\infty = 0$, and $dQ(\sqrt{2x}) = -(1/\sqrt{4\pi})$
 (e^{-x}/\sqrt{x}) . For Rayleigh fading channels, $m_1 = m_2 = 1$, and thus, (8)
is specialized to

$$\begin{aligned} P_e &= \frac{1}{\sqrt{4\pi}} \int_0^\infty \left[1 - 2e^{-\left(\frac{1}{\bar{\gamma}_1} + \frac{1}{\bar{\gamma}_2}\right)x} \sqrt{x(x+1)/\bar{\gamma}_1/\bar{\gamma}_2}\right. \\ &\quad \left. \cdot K_{-1} \left(2\sqrt{x(x+1)/\bar{\gamma}_1/\bar{\gamma}_2}\right)\right]^N \frac{e^{-x}}{\sqrt{x}} dx \end{aligned} \quad (9)$$

by replacing m_1 and m_2 in (5) with 1 and using the replaced expres-
sion of $F_{\gamma_k}^N(x)$ in (8). When x is large, $K_{-1}(x) \approx (1/x)$. Using this,
(9) can be approximated as

$$P_e \approx \frac{1}{2} + \frac{1}{2} \sum_{i=1}^N \frac{\binom{N}{i} (-1)^i}{\sqrt{1+i/\bar{\gamma}_1+i/\bar{\gamma}_2}}. \quad (10)$$

Equations (8) and (9) can be numerically calculated with only one
single integral, whereas (10) is calculated in closed form. All of them
are new results that are not available in the literature. They will be used
as benchmarks to compare different partial selection schemes.

B. Conventional Partial Selection Scheme

In [12], the conventional partial selection scheme chooses the idle
user according to

$$K = \max_{k=1,2,\dots,N} \{\gamma_{1,k}\} \quad (11)$$

by using the instantaneous SNR of the first hop only. Denote this
scheme as the $\max\{\gamma_{1,k}\}$ scheme. The $\max\{\gamma_{1,k}\}$ scheme greatly
reduces the complexity of cooperative diversity. The results in [12] are
for Rayleigh fading channels. We extend them to Nakagami- m fading
channels. Similar to (4), the probability of error in this case is given
by $P_e = \int_0^\infty P(e|x) dF_{\gamma_K}(x)$, where $P(e|x)$ is again the conditional
probability of error, which is conditioned on the instantaneous end-to-
end SNR of the chosen link γ_K , and $F_{\gamma_K}(x)$ is the cdf of γ_K derived
in the Appendix as

$$\begin{aligned} F_{\gamma_K}(x) &= 1 + \sum_{i=1}^N \sum_{j_i=0}^{m_1-1} \sum_{l_1=0}^{m_2-1} \sum_{l_2=0}^{j_1+\dots+j_i} 2(-1)^i m_2^{m_2} \binom{N}{i} \\ &\frac{\binom{m_2-1}{l_1} \binom{j_1+\dots+j_i}{l_2} [(m_1-1)!]^i}{\Gamma^i(m_1) \bar{\gamma}_2^{m_2} \Gamma(m_2) j_1! \dots j_i!} \\ &\cdot \left(\frac{m_2}{\bar{\gamma}_2}\right)^{\frac{l_2-l_1-1}{2}} \left(\frac{m_1}{\bar{\gamma}_1}\right)^{\frac{l_1-l_2+1}{2}+j_1+\dots+j_i} \\ &\cdot \frac{l_1-l_2+1}{2} x^{j_1+\dots+j_i+m_2-1-l_1+\frac{l_1-l_2+1}{2}} \end{aligned}$$

$$\begin{aligned} & \cdot (x+1)^{\frac{l_1+l_2+1}{2}} e^{-\left(\frac{im_1}{\bar{\gamma}_1} + \frac{m_2}{\bar{\gamma}_2}\right)x} \\ & \times K_{l_1-l_2+1} \left(2\sqrt{\frac{im_1m_2x(x+1)}{\bar{\gamma}_1\bar{\gamma}_2}} \right). \end{aligned} \quad (12)$$

144 Similarly, using integration by parts, one has

$$P_e = P(e|x)F_{\gamma_K}(x)_0^\infty - \int_0^\infty F_{\gamma_K}(x)dP(e|x). \quad (13)$$

145 For BPSK, one has $P(e|x) = Q(\sqrt{2x})$, $Q(\sqrt{2x})F_{\gamma_K}(x)_0^\infty = 0$ and
146 $dQ(\sqrt{2x}) = -(1/\sqrt{4\pi})(e^{-x}/\sqrt{x})$. Then, the error rate in (13) can
147 be calculated as

$$P_e = \frac{1}{\sqrt{4\pi}} \int_0^\infty F_{\gamma_K}(x) \frac{e^{-x}}{\sqrt{x}} dx \quad (14)$$

148 where $F_{\gamma_K}(x)$ is given by (12). Again, in Rayleigh fading channels, by
149 replacing m_1 and m_2 with 1 in (12) and using the replaced expression
150 in (14), (14) is specialized to

$$P_e = \frac{1}{\sqrt{4\pi}} \int_0^\infty \left[1 + \frac{1}{\bar{\gamma}_2} \sum_{i=1}^N \binom{N}{i} (-1)^i e^{-\frac{ix}{\bar{\gamma}_1} - \frac{x}{\bar{\gamma}_2}} \right. \\ \left. \sqrt{\frac{4\bar{\gamma}_2 ix(x+1)}{\bar{\gamma}_1}} K_1 \left(2\sqrt{\frac{i(x+1)x}{\bar{\gamma}_1\bar{\gamma}_2}} \right) \right] \frac{e^{-x}}{\sqrt{x}} dx. \quad (15)$$

151 Using $K_1(x) = K_{-1}(x)$ and $K_{-1}(x) \approx (1/x)$ for large x , one can
152 also approximate (15) as

$$P_e \approx \frac{1}{2} + \frac{1}{2} \sum_{i=1}^N \frac{\binom{N}{i} (-1)^i}{\sqrt{1 + \frac{i}{\bar{\gamma}_1} + \frac{1}{\bar{\gamma}_2}}}. \quad (16)$$

153 It can be verified that (16) agrees with [12, eq. (14)]. Equations (14)
154 and (15) are also new results that are not available in the literature.
155 They will be used to compare with the new schemes.

156 C. New Partial Selection Schemes

157 In the conventional partial selection scheme, one chooses the idle
158 user with the strongest first-hop instantaneous SNR. One can also
159 derive a new partial selection scheme that chooses the idle user with
160 the strongest second-hop instantaneous SNR as

$$K = \max_{k=1,2,\dots,N} \{\gamma_{2,k}\}. \quad (17)$$

161 Denote this scheme as the $\max\{\gamma_{2,k}\}$ scheme. Note that the
162 $\max\{\gamma_{2,k}\}$ scheme chooses the link with the strongest second-
163 hop, which is not equivalent to choosing the second strongest link.
164 Similarly, in Nakagami- m fading channels, its probability of error
165 for BPSK is (14), except that the cdf of γ_K is derived in the
166 Appendix as

$$F_{\gamma_K}(x) = 1 + \sum_{i=1}^N \sum_{j_i=0}^{m_2-1} \sum_{l_1=0}^{m_1-1} \sum_{l_2=0}^{j_i} 2(-1)^i m_1^{m_1} \binom{N}{i} \\ \times \frac{\binom{m_1-1}{l_1} \binom{j_i+\dots+j_i}{l_2} [(m_2-1)!]^i}{\Gamma^i(m_2)\bar{\gamma}_1^{m_1}\Gamma(m_1)j_i!\dots j_i!} \\ \cdot \left(\frac{m_1}{\bar{\gamma}_1}\right)^{\frac{l_2-l_1-1}{2}} \left(\frac{m_2}{\bar{\gamma}_2}\right)^{\frac{l_1-l_2+1}{2}+j_i+\dots+j_i}$$

$$\begin{aligned} & \times i^{\frac{l_1-l_2+1}{2}} x^{j_1+\dots+j_i+m_1-1-l_1+\frac{l_1-l_2+1}{2}} \\ & \cdot (x+1)^{\frac{l_1+l_2+1}{2}} e^{-\left(\frac{im_2}{\bar{\gamma}_2} + \frac{m_1}{\bar{\gamma}_1}\right)x} \\ & \times K_{l_1-l_2+1} \left(2\sqrt{\frac{im_1m_2x(x+1)}{\bar{\gamma}_1\bar{\gamma}_2}} \right). \end{aligned} \quad (18)$$

In Rayleigh fading channels, the probability of error for BPSK is 167
168 given by

$$P_e = \frac{1}{\sqrt{4\pi}} \int_0^\infty \left[1 + \frac{1}{\bar{\gamma}_1} \sum_{i=1}^N \binom{N}{i} (-1)^i e^{-\frac{ix}{\bar{\gamma}_2} - \frac{x}{\bar{\gamma}_1}} \right. \\ \left. \times \sqrt{\frac{4\bar{\gamma}_1 ix(x+1)}{\bar{\gamma}_2}} K_1 \left(2\sqrt{\frac{i(x+1)x}{\bar{\gamma}_1\bar{\gamma}_2}} \right) \right] \frac{e^{-x}}{\sqrt{x}} dx \quad (19)$$

which can be approximated as

169

$$P_e \approx \frac{1}{2} + \frac{1}{2} \sum_{i=1}^N \frac{\binom{N}{i} (-1)^i}{\sqrt{1 + \frac{1}{\bar{\gamma}_1} + \frac{i}{\bar{\gamma}_2}}}. \quad (20)$$

The aforementioned selection schemes use the instantaneous SNRs 170
171 for selection. This requires channel estimators for $h_{1,k}$ or $h_{2,k}$ or 171
172 both, $k = 1, 2, \dots, N$. It is also effective to use the received sig- 172
173 nal amplitude for selection [18]. Thus, two new partial selection 173
174 schemes are

$$K = \max_{k=1,2,\dots,N} \{|u_k|\} \quad (21)$$

$$K = \max_{k=1,2,\dots,N} \{|y_k|\}. \quad (22)$$

175 Denote (21) as the $\max\{|u_k|\}$ scheme and (22) as the $\max\{|y_k|\}$ 175
176 scheme. The selection of the idle user is made at the base station in 176
177 a centralized network or at the group leader in a distributed network. 177
178 The decision will be broadcast by the base station or the group leader 178
179 to the source, the destination, and the idle users. The implementation 179
180 details are not shown as they are beyond the scope of this paper. 180

181 Assume that each real symbol transmission costs the same overhead 181
182 P and each channel estimation uses Q real symbols. The $\max\{|u_k|\}$ 182
183 scheme requires transmission of the N received real amplitudes at 183
184 the idle users for selection and $h_{1,K}$ and $h_{2,K}$ for demodulation. 184
185 The overhead costs $NP + 2QP$. The $\max\{|y_k|\}$ scheme requires 185
186 transmission of the N received real amplitudes at the destination for 186
187 selection, which requires N channel estimators from $h_{1,1}$ to $h_{1,N}$ 187
188 to calculate the amplification factors for forwarding the signals and 188
189 $h_{2,K}$ for demodulation. The overhead costs $NP + (N+1)QP$. The 189
190 $\max\{\gamma_{2,k}\}$ scheme requires transmission of the N complex channel 190
191 estimates from $h_{2,1}$ to $h_{2,N}$ for selection and $h_{1,K}$ for demodu- 191
192 lation. The overhead costs $2NP + (N+1)QP$. The conventional 192
193 $\max\{\gamma_{1,k}\}$ scheme requires transmission of the N complex channel 193
194 estimates from $h_{1,1}$ to $h_{1,N}$ for selection and $h_{2,K}$ for demodu- 194
195 lation. The overhead costs $2NP + (N+1)QP$. The full selection 195
196 scheme requires transmission of N complex channel estimates from 196
197 $h_{1,1}$ to $h_{1,N}$ and N complex channel estimates from $h_{2,1}$ to $h_{2,N}$ 197
198 for selection and demodulation. The overhead costs $4NP + 2NQP$. 198
199 Thus, the partial selection schemes are simpler than the full se- 199
200 lection scheme, the new $\max\{|u_k|\}$ and $\max\{|y_k|\}$ schemes are 200
201 simpler than the conventional $\max\{\gamma_{1,k}\}$ scheme, whereas the new 201
202 $\max\{\gamma_{2,k}\}$ scheme has the same complexity as the conventional 202
203 $\max\{\gamma_{1,k}\}$ scheme. Among the new schemes, the $\max\{|u_k|\}$ scheme 203
204 is simplest, the $\max\{|y_k|\}$ scheme is second simplest, and the 204
205 $\max\{\gamma_{2,k}\}$ scheme is most complicated. The complexity reduction 205

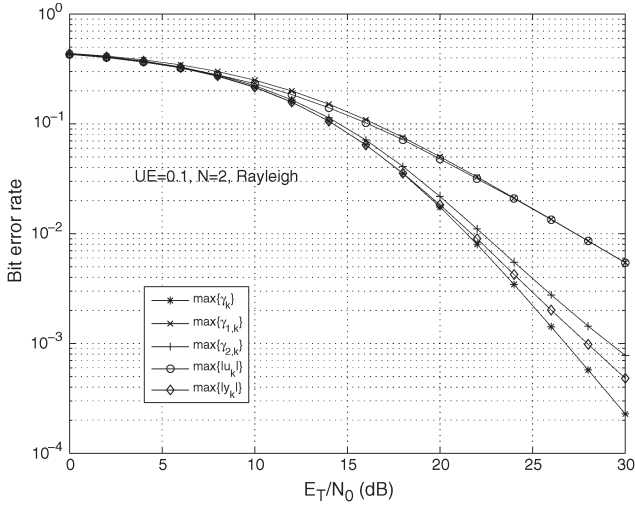


Fig. 1. Comparison of different partial selection schemes at $UE = 0.1$ and $N = 2$ in Rayleigh fading channels.

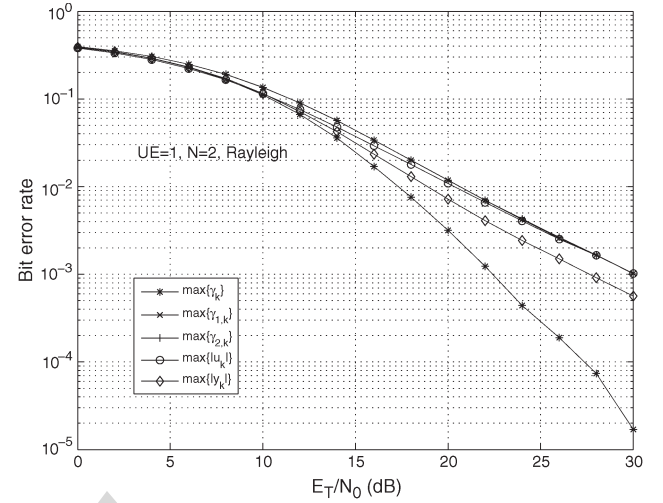


Fig. 3. Comparison of different partial selection schemes at $UE = 1$ and $N = 2$ in Rayleigh fading channels.

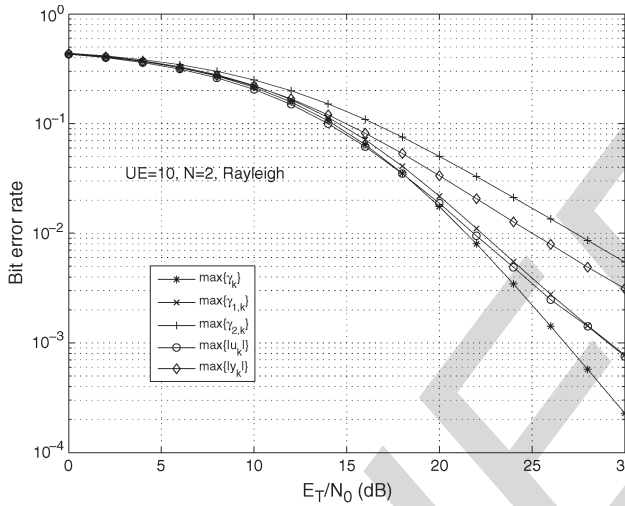


Fig. 2. Comparison of different partial selection schemes at $UE = 10$ and $N = 2$ in Rayleigh fading channels.

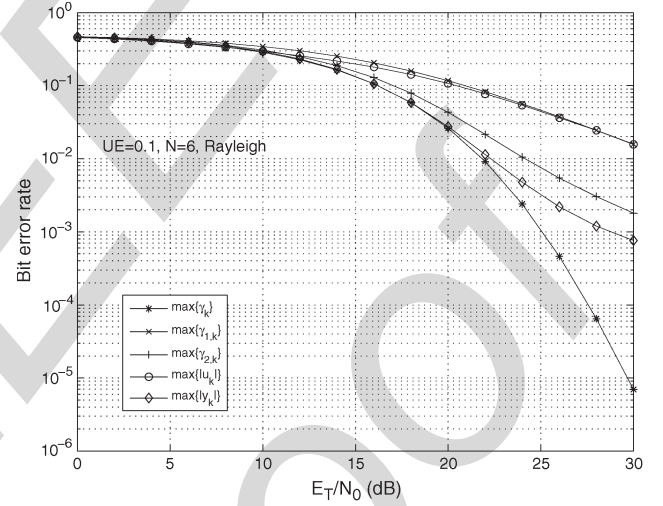


Fig. 4. Comparison of different partial selection schemes at $UE = 0.1$ and $N = 6$ in Rayleigh fading channels.

206 increases when N increases. Derivation of the error rate for amplitude-
207 based selection in (21) and (22) has been a long-standing problem
208 and is not available [19].

209 III. NUMERICAL RESULTS AND DISCUSSION

210 Here, numerical examples are presented to compare the perfor-
211 mances of different partial selection schemes. In the comparison,
212 BPSK is used. In addition, $\Omega_1 = \Omega_2 = 1$, and $N_1 = N_2 = N_0 = 1$,
213 whereas $E_1 = E_T/N(UE + 1)$, and $E_2 = E_T * UE/N(UE + 1)$,
214 where $*$ represents product, $E_T = (E_1 + E_2)N$ is the total energy, and
215 $UE = E_2/E_1$ is the ratio of E_2 to E_1 . Since $\Omega_1 = \Omega_2$ and $N_1 = N_2$,
216 UE is also the ratio of $\bar{\gamma}_2$ to $\bar{\gamma}_1$.

217 Fig. 1 compares different partial selection schemes when $N = 2$
218 and $UE = 0.1$ in Rayleigh fading channels. One sees that all the
219 new partial selection schemes outperform the conventional $\max\{\gamma_{1,k}\}$
220 scheme. For example, at a bit error rate of 10^{-2} , the new $\max\{\gamma_{2,k}\}$
221 and $\max\{|y_k|\}$ schemes have performance gains of around 5 dB
222 over the conventional $\max\{\gamma_{1,k}\}$ scheme. Comparing the new partial
223 selection schemes, one sees that the $\max\{|y_k|\}$ scheme performs
224 the best. Its performance is indistinguishable from the performance
225 of the full selection $\max\{\gamma_k\}$ scheme when the SNR is less than

20 dB. Fig. 2 compares different partial selection schemes when
226 $N = 2$ and $UE = 10$ in Rayleigh fading channels. In this case, the
227 new $\max\{|u_k|\}$ scheme still outperforms the conventional $\max\{\gamma_{1,k}\}$
228 scheme. Among the new schemes, the $\max\{|u_k|\}$ scheme performs
229 the best. Since the second hop has a smaller average SNR ($\bar{\gamma}_2 = 230$
230 $0.1\bar{\gamma}_1$) in Fig. 1 and the first hop has a smaller average SNR ($\bar{\gamma}_2 = 231$
231 $10\bar{\gamma}_1$) in Fig. 2, one concludes that one should choose the best idle user
232 for the hop with a smaller average SNR to achieve maximum bit error
233 rate performance in partial selection. This may be explained as follows:
234 The value of γ_k approaches $\gamma_{1,k}$ when $\gamma_{2,k}$ is large, and it approaches
235 $\gamma_{2,k}$ when $\gamma_{1,k}$ is large. Thus, it is necessary to make choices in the
236 weaker hop on average. Fig. 3 compares different partial selection
237 schemes when $N = 2$ and $UE = 1$ in Rayleigh fading channels. In
238 this case, both hops have the same average SNR. One sees that both the
239 new $\max\{|u_k|\}$ and $\max\{|y_k|\}$ schemes outperform the conventional
240 $\max\{\gamma_{1,k}\}$ scheme, whereas the performance of the new $\max\{\gamma_{2,k}\}$
241 scheme is graphically indistinguishable from the performance of the
242 conventional $\max\{\gamma_{1,k}\}$ scheme. In addition, the $\max\{|y_k|\}$ scheme
243 performs the best among the new schemes. 244

245 Fig. 4 compares different schemes when $N = 6$ and $UE = 0.1$ in
246 Rayleigh fading channels. Similar observations to those from Fig. 1
247 can be made. In addition, the performance of the full selection 248

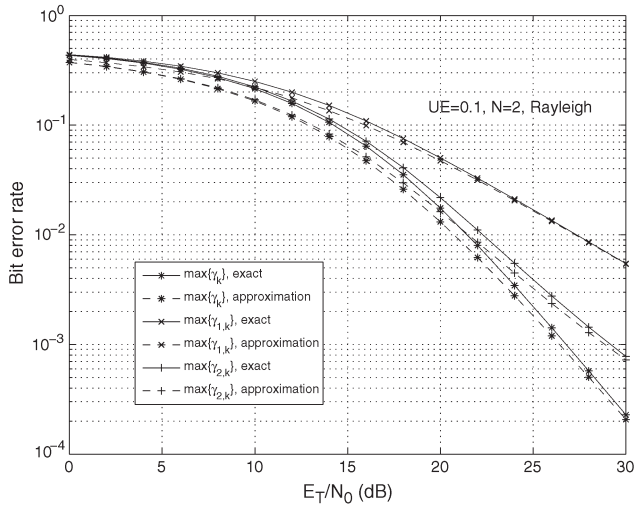


Fig. 5. Comparison of the exact error rates and the approximate error rates for different partial selection schemes at $UE = 0.1$ and $N = 2$ in Rayleigh fading channels.

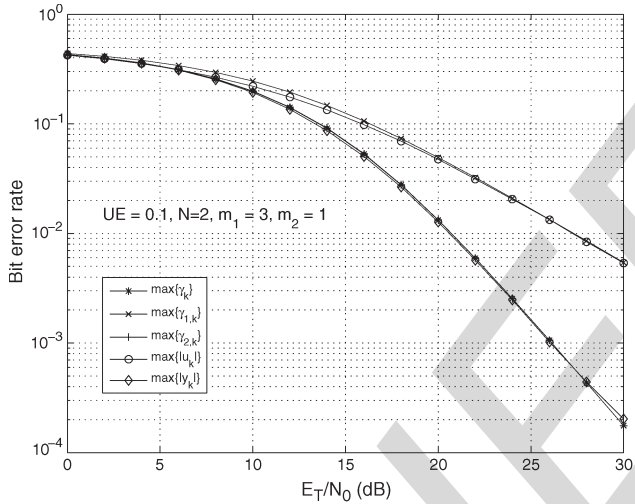


Fig. 6. Comparison of different partial selection schemes at $UE = 0.1$, $N = 2$, $m_1 = 3$, and $m_2 = 1$ in Nakagami- m fading channels.

248 scheme improves when N increases, whereas the performances of
 249 the partial selection schemes do not. This is due to the fact that
 250 the full selection scheme has a diversity order of N , whereas the
 251 partial selection scheme has a diversity order of only 1 to achieve
 252 lower complexity. Fig. 5 compares the exact performances of the
 253 $\max\{\gamma_k\}$, $\max\{\gamma_{1,k}\}$, and $\max\{\gamma_{2,k}\}$ schemes with their approx-
 254 imate performances in (10), (16), and (20), respectively. One sees
 255 that the approximation error decreases when the SNR increases.
 256 Therefore, the approximations in (10), (16), and (20) can be used to
 257 predict the asymptotic performances, which are defined as the system
 258 performances when the SNR approaches infinity. Fig. 6 compares
 259 different schemes in Nakagami- m fading channels at $UE = 0.1$,
 260 $m_1 = 3$, and $m_2 = 1$. In this example, all the new partial selection
 261 schemes outperform the conventional $\max\{\gamma_{1,k}\}$ scheme. In particu-
 262 lar, the performances of the $\max\{\gamma_{2,k}\}$ and $\max\{|y_k|\}$ schemes are
 263 almost identical to that of the full selection scheme. This agrees with
 264 previous observations from Figs. 1 and 2 that the best idle user for
 265 the hop with a smaller average SNR should be chosen as $\bar{\gamma}_2 = 0.1\bar{\gamma}_1$.
 266 However, when $\bar{\gamma}_2 = 0.1\bar{\gamma}_1$ but $m_2 > m_1$, as shown in Fig. 7, one sees
 267 that the best idle user for the hop with a smaller m parameter should
 268 be chosen at large SNRs, as the $\max\{\gamma_{1,k}\}$ and $\max\{|u_k|\}$ schemes
 269 outperform the $\max\{\gamma_{2,k}\}$ and $\max\{|y_k|\}$ schemes at large SNRs,

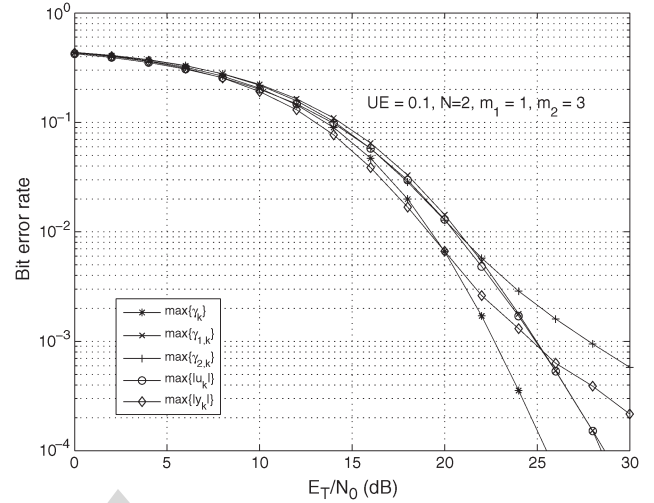


Fig. 7. Comparison of different partial selection schemes at $UE = 0.1$, $N = 2$, $m_1 = 1$, and $m_2 = 3$ in Nakagami- m fading channels.

despite the fact that $\bar{\gamma}_2 = 0.1\bar{\gamma}_1$. One also notes that the $\max\{|y_k|\}$ 270
 scheme outperforms the $\max\{\gamma_k\}$ scheme for small SNRs. This was 271
 also observed in [18], where selection based on amplitude outperforms 272
 that based on SNR. It has been explained in [18] that the orientation 273
 of the noise vector may improve the performance of amplitude-based 274
 selection. 275

One concludes from Figs. 1–7 that, if the m parameters are the same 276
 for both hops, the best idle user for the hop with a smaller average SNR 277
 should be chosen. On the other hand, if the m parameters are different 278
 for the two hops, the best idle user for the hop with a smaller average 279
 SNR should be chosen at small SNRs and that with a smaller m 280
 parameter should be chosen at large SNRs. This observation motivates 281
 a new adaptive partial selection scheme by choosing the instantaneous 282
 SNR or the received signal amplitude of either the first hop or the 283
 second hop according to their average SNRs and m parameters. This 284
 scheme outperforms schemes using either the first hop or the second 285
 hop alone, at the cost of extra knowledge of the average SNR and the 286
 m parameter, which can be accurately estimated using [15]. 287

APPENDIX

DERIVATION OF (12) AND (18)

In the $\max\{\gamma_{1,k}\}$ scheme, one has the instantaneous end-to-end 290
 SNR of the chosen link as 291

$$\gamma_K = \frac{\gamma_{1,K}\gamma_{2,K}}{\gamma_{1,K} + \gamma_{2,K} + 1} \quad (23)$$

where $\gamma_{1,K} = \max_{k=1,2,\dots,N}\{\gamma_{1,k}\}$, and $\gamma_{2,K}$ is the instantaneous 292
 SNR in the second hop of the chosen link. The cdf of $\gamma_{1,K}$ can be 293
 derived as $F_{\gamma_{1,K}}(x) = [1 - (\Gamma(m_1, m_1 x / \bar{\gamma}_1) / \Gamma(m_1))]^N$, where 294
 $\Gamma(\cdot, \cdot)$ is the incomplete Gamma function [17, eq. (8.350.2)]. The 295
 pdf of $\gamma_{2,K}$ is $f_{\gamma_{2,K}}(x) = (m_2^{m_2} x^{m_2-1} / \bar{\gamma}_2^{m_2} \Gamma(m_2)) e^{-(m_2/\bar{\gamma}_2)x}$. 296
 Following similar methods in [16], the cdf of γ_K is 297

$$\begin{aligned} F_{\gamma_K}(x) &= \int_0^\infty Pr \left\{ \frac{x_1 x_2}{x_1 + x_2 + 1} \leq x | x_2 \right\} f_{\gamma_{2,K}}(x_2) dx_2 \\ &= \int_0^x f_{\gamma_{2,K}}(x_2) dx_2 \end{aligned}$$

$$\begin{aligned}
& + \int_x^\infty F_{\gamma_{1,K}} \left(\frac{x(x_2+1)}{x_2-x} \right) f_{\gamma_{2,K}}(x_2) dx_2 \\
= & 1 + \sum_{i=1}^N \frac{(-1)^i m_2^{m_2} \binom{N}{i}}{\Gamma^i(m_1) \bar{\gamma}_2^{m_2} \Gamma(m_2)} \\
& \times \int_x^\infty \Gamma^i \left(m_1, \frac{m_1 x(x_2+1)}{\bar{\gamma}_1(x_2-x)} \right) x_2^{m_2-1} e^{-\frac{m_2}{\bar{\gamma}_2} x_2} dx_2.
\end{aligned} \tag{24}$$

298 Using [17, eq. (8.352.2)] and [17, eq. (3.471.9)] and after some math-
299 ematical manipulations, one has (12). When the $\max\{\gamma_{2,k}\}$ scheme is
300 used, the instantaneous end-to-end SNR of the chosen link is

$$\gamma_K = \frac{\gamma_{1,K} \gamma_{2,K}}{\gamma_{1,K} + \gamma_{2,K} + 1} \tag{25}$$

301 where $\gamma_{2,K} = \max_{k=1,2,\dots,N} \{\gamma_{2,k}\}$, and $\gamma_{1,K}$ is the instantaneous
302 SNR in the first hop of the chosen link. Due to symmetry, one can
303 obtain (18).

304

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