A Non-Stationary MIMO Channel Model for High-Speed Train Communication Systems

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Abstract—This paper proposes a non-stationary wideband geometry-based stochastic model (GBSM) for multiple-input multiple-output (MIMO) high-speed train (HST) channels. The proposed model has the ability to investigate the non-stationarity of HST environment caused by the high speed movement of the receiver. Based on the proposed model, the space-time-frequency (STF) correlation function (CF) and STF local scattering function (LSF) are derived for different taps. Numerical results show the non-stationarity of the proposed channel model.

I. INTRODUCTION

Due to the growing demand for broadband services in the area of passenger transport, the implementation of wireless communication systems in HSTs has attracted great interest from communication companies. The existing wireless communication system for railways, Global System for Mobile Communication Railway (GSM-R), cannot meet the requirements for high transmission rates to satisfy the demands of current broadband users, besides the fact that GSM-R is used for train control rather than providing communications for train passengers. Using current candidates for the fourth generation (4G) wireless systems such as IMT-Advanced (IMT-A) [1] and Long Term Evolution-Advanced (LTE-A) [2] needs to overcome various challenges that face these systems in high mobility environments. Challenges like fast handover [3], high penetration losses [4], and limited visibility in tunnels [5], besides the varying Doppler, delay, and angular spreads [6] due to the high-speed link between transmitters and receivers, need to be addressed. Therefore, investigations into radio propagation characteristics for wireless communication systems that are capable of providing broadband communications in HSTs have been initiated.

The key features of wireless channels in HST communication systems are time-varying and non-stationarity. Although several measurement campaigns have been conducted for high-velocity scenarios [7]–[11] but they mainly focused on large scale parameters like path loss and the root mean square (RMS) delay spread and ignored other propagation characteristics. Table 1 classifies some of the HST measurement campaigns according to carrier frequencies, bandwidth, antennas, measured channel and channel statistics.

On the other hand, channel models in the literature have also failed to characterize different propagation parameters of similar scenarios. 3GPP defines a channel model for high-speed train tests in LTE-A. However, this model is a non-fading propagation channel model and consists of one ray only. It mainly concentrates on studying the impact of Doppler effect on system performance while ignoring other channel characteristics. WINNER-II [12] and IMT-A channel models also consider high-speed scenarios in their rural macro-cell (RMs) and moving networks scenarios, respectively, where the MS antenna speed is in the range of 0 – 350 km/h. The proposed scenario considers dedicated mobile relay stations (MRSs) deployed on the surface of the train to improve the coverage on the carriages by extending the coverage of the outdoor base stations (BSs). Therefore, two types of channels can be distinguished, i.e., BS-MRS and MRS-mobile station (MS) channels. IMT-A considers that the BS-MRS channel satisfies the assumption of wide-sense stationary uncorrelated scattering (WSSUS) neglecting the non-stationarity of this channel. It also considers an MRS-MS channel as an indoor one ignoring the effect of the surrounding environment. As indicated in [8], waves re-entering the carriage from outside of the train can be dominant in certain cases. It also showed that the propagation loss in a train carriage can be less than the free space one due to the waveguide effect in a closed space environment like trains. In [6] and [13], the propagation channels between HSTs and fixed BSs were modeled using the ray-tracing method which incorporates a detailed simulation of the actual physical wave propagation process based on Maxwell equations. The authors presented two-dimensional (2D) ray-tracing [6] and three-dimensional (3D) ray-tracing [13] channel models to investigate the effects of different antenna types on the channel impulse response and how to reduce the inter-carrier interference (ICI) and inter-symbol interference (ISI). However, the implementation of ray-tracing models always requires extensive computational resources.
The aforementioned examples have motivated us to investigate more thoroughly the parameters that distinguish the HST scenario from other propagation scenarios and to design an accurate channel model that is able to mimic the key parameters of similar radio environments.

The rest of this paper is organized as follows. A GBSM for MIMO HST channels is proposed in Section II. In Section III, the STF CF and LSF of the GBSM are derived. The numerical results and the analysis are presented in Section IV. Finally, the conclusions are drawn in Section V.

II. THE GBSM

We consider a MIMO HST communication system with $S$ transmit and $U$ receive omni-directional antenna elements. The BS is considered to be located on the track-side ($D_{\min} = 2m$) as in [1]. Both the BS and MRS are equipped with multiple antennas at equivalent heights as shown in Fig. 1. Fig. 2 illustrates the geometry of the proposed GBSM, which consists of multiple confocal ellipses with single-bounced rays and the line-of-sight (LoS) component [15]. For clarity purposes, in this figure, we use a 2x2 MIMO channel model as an example. The multiple confocal ellipses model with the BS and MRS located at the foci represents the tapped delay line (TDL) structure and has $N$ effective scatterers on the path between the BS and MRS, as in [1]. Both the BS and MRS are equipped with multiple antennas. The angle-of-arrival (AoA) of the wave traveling from an effective scatterer on the MRS can be expressed as in [16]. Both the BS and MRS are equipped with multiple antennas.

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Let the discrete propagation delay of the $i$th tap, respectively. From Fig. 2 and based on the law of cosines, we have $\phi_{i}^{(n)}$ and $\phi_{R}^{(n)}$ designate the Ricean factors. The phases $\psi_{n}$ and $\psi_{n}$ are independent and identically distributed (i.i.d.) random variables with uniform distributions over $[-\pi, \pi]$ and $f_{\max}$ is the maximum Doppler frequency with respect to the MRS.

From Fig. 2 and based on the law of cosines, we have $\phi_{i}^{(n)} = \frac{D_{s} - v_{t}}{D_{s} - v_{t}}$, and $\phi_{R}^{(n)} = \frac{D_{s} - v_{t}}{D_{s} - v_{t}}$. The time-variant LoS AoA $\phi_{i}^{(n)}$ can be expressed as [2]

$$\phi_{i}^{(n)}(t) = \frac{\text{arccos} \left( \frac{D_{s} - v_{t}}{D_{s} - v_{t}} \right)}{\text{arccos} \left( \frac{-1.5D_{s} + v_{t}}{D_{s} - v_{t}} \right)}, \quad 0 \leq t \leq \frac{2D_{s}}{v_{t}},$$

$$\phi_{R}^{(n)}(t) = \frac{\text{arccos} \left( \frac{D_{s} - v_{t}}{D_{s} - v_{t}} \right)}{\text{arccos} \left( \frac{-1.5D_{s} + v_{t}}{D_{s} - v_{t}} \right)}, \quad \frac{2D_{s}}{v_{t}} < t \leq \frac{4D_{s}}{v_{t}},$$

$$\phi_{i}^{(n)}(t) = \frac{2D_{s}}{v_{t}} \text{ mod } \frac{2D_{s}}{v_{t}}.$$
Since the numbers of effective scatterers are assumed to be infinite, i.e., \( N \rightarrow \infty \), the proposed model is actually a mathematical reference model. Due to the infinite complexity, a reference model cannot be implemented in practice. A reference model can be used for theoretical analysis and design of a communication system, and as a starting point to design a reliable simulation model that has the reasonable complexity, i.e., with finite values of \( N \). Here, we use the von Mises PDF defined as \( f(\phi) = \frac{e^{\kappa \cos(\phi - \mu)}}{2\pi I_0(\kappa)} \), where \( \phi \in [-\pi, \pi] \), \( I_0(\cdot) \) is the zeroth-order modified Bessel function of the first kind, \( \mu \in [-\pi, \pi] \) accounts for the mean angular value of the angle \( \phi \), and \( \kappa (k \geq 0) \) is a real-valued parameter that controls the spread of the \( \phi \). For the continuous AoAs \( \phi_{iQ}^{t} \in [-\pi, \pi] \) and AoDs \( \phi_{qP}^{t} \in [-\pi, \pi] \), the relevant parameters in the von Mises PDF are \( \mu_{R}^{i} \) and \( k_{R}^{i} \) and \( \mu_{P}^{t} \) and \( k_{P}^{t} \), respectively. In case of isotropic scattering, \( k = 0 \), the von Mises distribution reduces to the uniform function \( f(\phi) = 1/(2\pi) \).

III. CHARACTERIZATION OF THE HST CHANNEL MODEL

Unlike non-stationary channels [17], characterization of WSSUS channels has been investigated thoroughly in the literature [18], [19]. For the proposed non-stationary HST GBSM, we can obtain the corresponding time-varying transfer function by taking the Fourier transformation of the complex impulse response \( h_{pq}(t, \tau') \) in terms of \( \tau' \), i.e.,

\[
L_{H_{pq}}(t, f) = \int h_{pq}(t, \tau') e^{-j2\pi f \tau'} d\tau'
\]

which essentially is a non-stationary process for HST scenarios. The channel correlations/nonstationarities that have been described in [20] can be extended to an STF CF and expressed as

\[
R_{L[1]pq}^{L[1]pq}(t, f; \Delta t, \Delta f) = \mathbb{E}[L_{H_{pq}}(t, f + \Delta f) L_{H_{pq}}^{*}(t - \Delta t, f)]
\]

where \((\cdot)^{*}\) denotes the complex conjugate operation, \( \mathbb{E}[\cdot] \) designates the statistical expectation operator, \( \Delta t \) and \( \Delta f \) denote the time lag and frequency lag, respectively. The LSF describes the mean power of the effective scatterers that cause delay-Doppler shifts \( (\tau, \nu) \) at time \( t \) and frequency \( f \). It is defined as a space-time-frequency dependant scattering function of the non-stationary process \( L_{H_{pq}}(t, f) \), i.e.,

\[
C_{H_{pq}}^{L}(t, f, \tau, \nu) = \int \int R_{L[1]pq}^{L[1]pq}(t, f; \Delta t, \Delta f) e^{-j2\pi(\nu(\Delta t - \tau) + \Delta f)}d\Delta t \Delta f.
\]

By applying the corresponding von Mises distribution, and the equality \( \int_{-\pi}^{\pi} \exp(a \sin c + b \cos c) dc = 2\pi I_0(\sqrt{a^2 + b^2}) \), we can obtain \( R_{L}(t, f; \Delta t, \Delta f) \) of the LoS and single-bounced components of different taps as follows.

1) In the case of the LoS component

\[
R_{LL[1]pq}^{LL[1]pq}(t, f; \Delta t, \Delta f) = K_{pq} e^{j2\pi(G + \Delta t W(t) - \Delta f \tau_1)}
\]

where \( G = P \cos\beta_T - Q \cos\beta_R \), with \( P = (y' - y) \delta_T/\lambda \), \( Q = (q' - q) \delta_R/\lambda \), \( W(t) = \max j \cos \left( \phi_{L}(t) - \gamma_R \right) \), and \( K' = \sqrt{\frac{K_{pq}}{(K_{pq} + 1)(K_{pq} + 1)}} \).

2) In the case of the single-bounced components

\[
R_{LSUSS}^{LSUSS}(t, f; \Delta t, \Delta f) = \frac{1}{2\pi I_0(K_{pq}^{i}) U} \int_{-\pi}^{\pi} e^{j2\pi K_{pq}^{i} \cos(\phi_{L}(t) + \mu_{R}^{i})} \frac{P \cos(\phi_{L}(t) + \beta_{R}) + Q \cos(\phi_{L}(t) - \beta_{R})}{\cos(\phi_{L}(t) - \gamma_{R})} e^{-j2\pi f \tau_1}
\]

where \( K_{pq}^{i} \) and \( U = \sqrt{(K_{pq}^{i} + 1)(K_{pq}^{i} + 1)} \) only appear for the first tap. Substituting (11) and (13) into (9), we can obtain the corresponding LSFs.

IV. NUMERICAL RESULTS AND ANALYSIS

In this section, the analytical expressions provided in the previous section are evaluated numerically. From the moving networks scenario in [12] that was designed based on some measurements in HST environments, we have chosen the following parameters: the LoS Ricean factor \( K_{pq} = K_{pq}^{i} \) = 6 dB, taps delay for the first and second tap are \( \tau_1 = 0 \) and \( \tau_2 = 50 \) ns, respectively, \( f_c = 6 \) GHz, \( v = 360 \) km/h, \( f_{max} = 2 \) kHz, \( D_s = 500 \) m, \( a_1 = \frac{D_s}{2} + 150 \) m, \( a_2 = \frac{D_s}{2} + 180 \) m, \( \gamma_R = 0 \) and we are using a uniform antenna array with \( M_R = M_T = 2 \) and \( \beta_R = \beta_T = \pi/2 \). Figs. 3 and 4 show the absolute values of the theoretical STF CFs \( R_{L[1]pq}^{L[1]pq}(t, f; \Delta t, \Delta f) \) of the proposed HST model for the first tap and second tap, respectively, when considering an isotropic environment \( k_{pq} = 0 \) and adopting a BS antenna elements spacing \( \delta_T = \lambda \). We can see that the STF CF changes for different values of \( t \), which is due to the non-stationary
of the channel model. Fig. 3 shows higher correlations than Fig. 4 proving that the LoS component, which is dominant in HST scenarios [1], [2] and [12], increases the correlation between different antenna elements and as a result it reduces the benefit of using MIMO techniques in such environments.

The absolute values of the normalized STF LSF of the second tap of the channel model \( c_H^{\text{STF}} (t, f, \tau, \nu) \) are shown in Fig. 5. It can be seen from this figure how the power of the effective scatters varies with time \( t \). It can also be noticed that the power of components with zero Doppler frequency is higher than the rest of the components for all time instants \( t \).

The normalized STF LSF of the proposed HST model for different taps with delays \( \tau_i \) at a certain time instant and with the assumption of no correlation between different taps is reduced to Doppler power spectrum density (PSD) function which is illustrated in Fig. 6. From this figure, we can see that different taps have the same classic Doppler spectrum at a certain time instant and with \( i \).

V. CONCLUSIONS

Non-stationary channel models are increasingly important for designing and evaluating different proposed solutions for future HST communication systems. In this paper, we have proposed a non-stationary wideband MIMO HST GBSM that takes into account the LoS component and single-bounced rays. The proposed channel model enables us to study the time-varying channel statistics. From this model, we have derived the STF CFs and STF LSFs for different taps. Numerical results have proved that the stationary assumption is violated for HST channels.

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REFERENCES


TABLE I

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<tr>
<th>Meas. Channel</th>
<th>Carrier Frequency</th>
<th>Bandwidth</th>
<th>Antenna</th>
<th>Channel Statistics</th>
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<tbody>
<tr>
<td>Indoor</td>
<td>2.35 GHz</td>
<td>100 MHz</td>
<td>SISO</td>
<td>PL, DS, K</td>
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<tr>
<td>Inter-car</td>
<td>5.2 GHz/2.2 GHz</td>
<td>20 MHz</td>
<td>SISO</td>
<td>PL</td>
</tr>
<tr>
<td>O2I</td>
<td>2.154 GHz</td>
<td>30 MHz</td>
<td>SISO</td>
<td>PL, DS</td>
</tr>
<tr>
<td>O2I</td>
<td>2.5 GHz</td>
<td>50 MHz</td>
<td>MISO</td>
<td>DS, AnA, PAS, DF</td>
</tr>
<tr>
<td>O2I</td>
<td>930 MHz</td>
<td>N/A</td>
<td>SIFO</td>
<td>PL, SF</td>
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<td>O2I: outdoor-to-indoor</td>
<td>120 MHz</td>
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HST CHANNEL MEASUREMENTS.
Fig. 1. A HST communication system.

Fig. 2. The GBSM for a MIMO HST channel.

Fig. 3. The absolute values of the non-stationary STF CF of the first tap of the proposed HST channel model.

Fig. 4. The absolute values of the non-stationary STF CF of the second tap of the proposed HST channel model.

Fig. 5. The absolute values of the non-stationary STF LSF of the second tap of the proposed HST channel model.

Fig. 6. The normalized STF LSF of the proposed HST channel model of different taps at a certain time \((t = 0)\).