

# Coverage in Heterogeneous Networks

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# Introduction



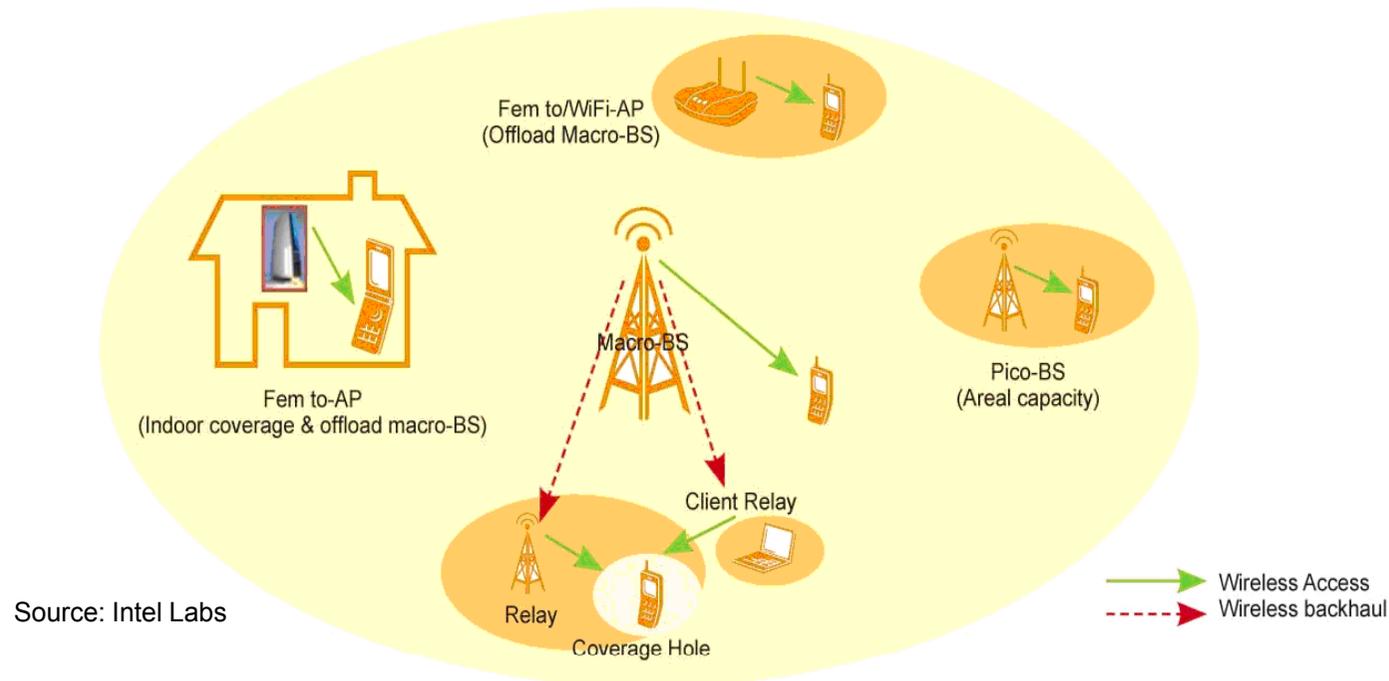
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# Why Heterogeneous?

- Needs for substantial improvements in cellular capacity and coverage
  - Radio link improvement alone cannot meet increasing demands
  - Traffic demand and channel condition vary with time and location
- Improve spectral efficiency/area/cost
  - Need to increase cell density cost-effectively
  - Network topology provides gains beyond radio technology
- Heterogeneous networks
  - Deploy macro-, pico-, femto-cells, and relays in the same spectrum
  - Improve coverage and capacity through better spatial reuse
  - Address hot-spot needs and coverage holes
  - Lower traffic load on macrocells

# Deployment

- Initial coverage with macro base stations (MBS)
- Add pico, femto and relay stations for capacity increase, hot spots, indoor coverage, etc.
- Pico, femto and relay stations require lower power, offer flexible site acquisition, and add little or no backhaul expense.

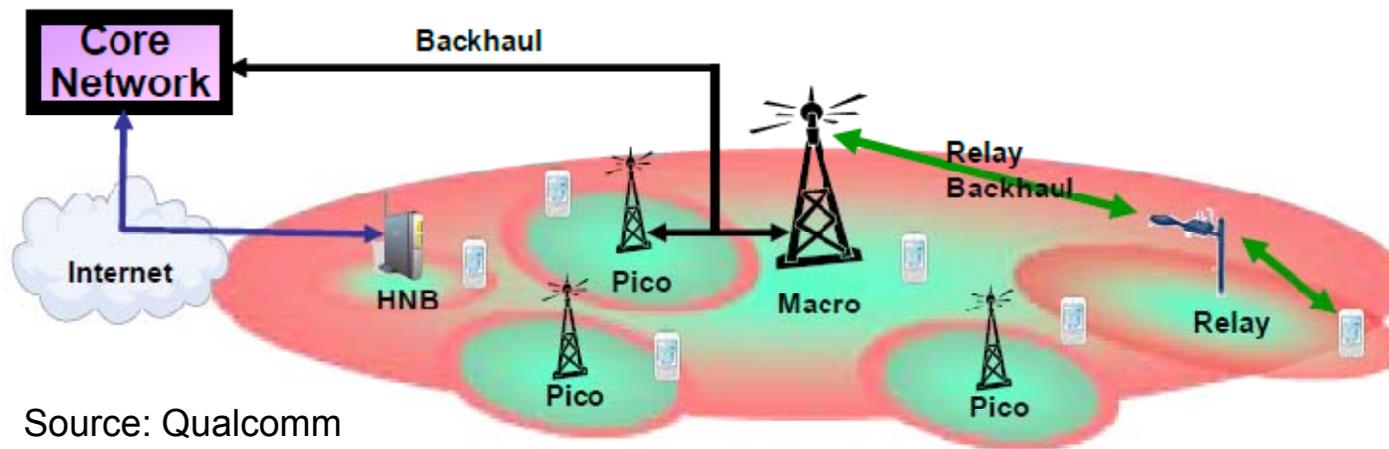


# Heterogeneous Networks

- **Macrocells**
  - Operator-deployed BSs use dedicated backhaul
  - Open to public access
  - $P_{Tx} \sim 43$  dBm,  $G \sim 12-15$  dBi
- **Picocells**
  - Operator-deployed BSs use dedicated backhaul
  - Open to public access
  - $P_{Tx} \sim 23-30$  dBm,  $G \sim 0-5$  dBi
- **Femtocells**
  - User-deployed BSs use user's broadband connection as backhaul
  - Open access, closed access, or a hybrid access policy
  - $P_{Tx} \leq 23$  dBm,  $G \sim 0-2$  dBi
- **Relays**
  - Operator-deployed BSs use over-the-air link to MBS as backhaul
  - $P_{Tx} \sim 23-30$  dBm,  $G \sim 0-5$  dBi

# HN Characteristics

- Coexistence of potentially different access technologies
- Different cell scales: macro > micro > pico > femto
- BSs owned by operators, enterprises and consumers
- Wired or wireless backhaul with guaranteed or best-effort QoS
- Femtocells potentially offer coverage only to subscribed UEs



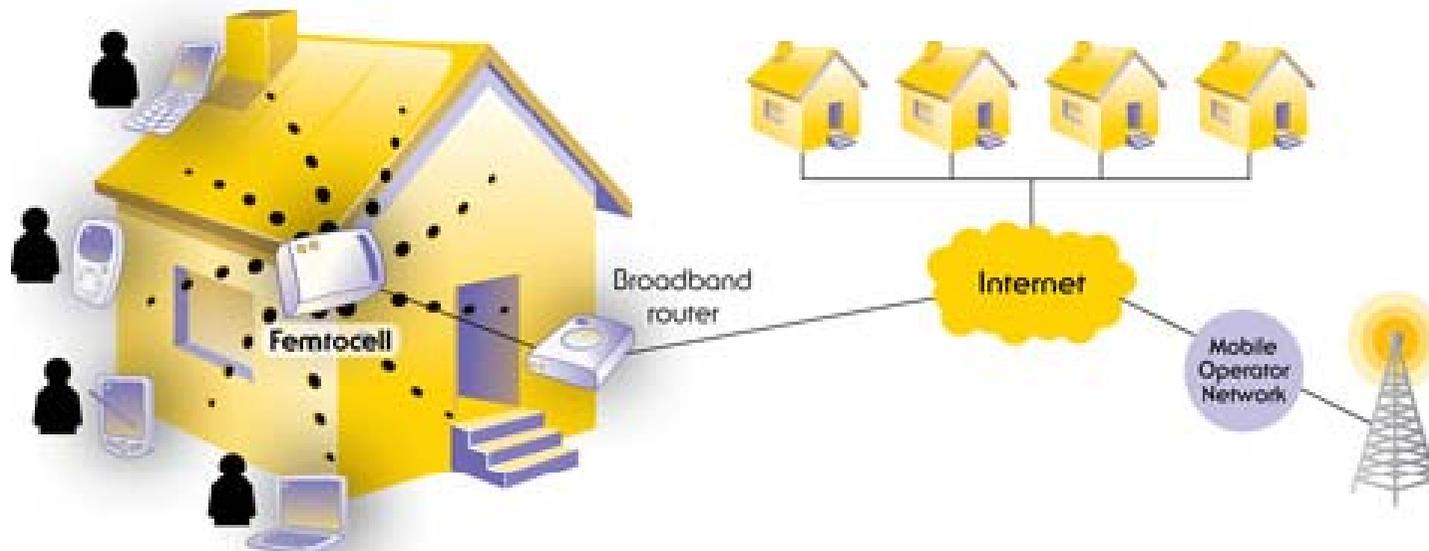
Source: Qualcomm

# Challenges

- Maintain uniform user experience
  - More cell-edges created
  - Near-far effect
  - Closed-access femtocells in co-channel deployments
  - Relay stations may have different duplexing schedules
- Handoff decisions have to consider backhaul capacity, especially for relays and femtocells
- Optimized use of radio resources
- Inter-cell interference management
  - Lack of coordination between cells
  - Scalability, security and limited backhaul bandwidth

# Femtocells

- Femtocells are low-power wireless access points that operate in licensed spectrum to connect standard mobile devices to a mobile operator's network using residential DSL or cable broadband connections [Source: Femto Forum].



# Coverage

- Inter-cell interference creates dead spots where UE QoS cannot be guaranteed.
  - Location w.r.t. MBS
  - Path loss, shadowing, fading
- Minimum distance of an FAP from the MBS s.t. a femto outage probability (OP) constraint
- Maximum density of simultaneously transmitting co-channel femtocells meeting a macro/femto OP constraint
- Maximum allowed transmit power of FAPs s.t. a macro OP constraint
- Minimum required transmit power of FAPs s.t. a femto OP constraint

# Coverage Analysis



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# System Model

- OFDMA downlink of collocated spectrum-sharing macrocell and closed-access femtocells
  - A central MBS covers a disc area with radius  $r_M$
  - Femtocells of radius  $r_F$  are randomly distributed on  $\mathbb{R}^2$  as a spatial Poisson point process (SPPP) with a density of  $\lambda_F$ .
  - $N_F$  femtocells per cell site on average
  - $U_F$  indoor UEs per femtocell, each located on cell edge
  - MBS transmit power is  $P_{M,Tx}$  per RB
  - FAP transmit power is  $P_{F,Tx}$  per RB
  - Each FAP transmits with a probability  $\rho$  within each RB.
  - Spatial intensity of simultaneously transmitting co-channel FAPs is  $u_F = \lambda_F \rho$ .

# Channel Model

- Each subchannel sees Rayleigh flat fading and lognormal shadowing
- Path loss follows the IMT-2000 channel model

- MBS to outdoor UE

$$PL_M = \phi_M D_M^{\alpha_M} = 10^{-7.1} f_c^3 D_M^{\alpha_M}$$

- MBS to indoor UE

$$PL_{FM} = \phi_{FM} D_{FM}^{\alpha_{FM}} = \phi_M \xi D_{FM}^{\alpha_{FM}} = 10^{-7.1} f_c^3 \xi D_{FM}^{\alpha_{FM}}$$

- Home FAP to indoor UE

$$PL_F = \phi_F D_F^{\alpha_F} = 10^{3.7} D_F^{\alpha_F}$$

- FAP to outdoor UE

$$PL_{MF} = \phi_{MF} D_{MF}^{\alpha_{MF}} = \phi_F \xi D_{MF}^{\alpha_{MF}}$$

- Interfering FAP to indoor UE

$$PL_{FF} = \phi_{FF} D_{FF}^{\alpha_{FF}} = \phi_F \xi^2 D_{FF}^{\alpha_{FF}}$$

- $\xi$  denotes wall-penetration loss

# Femto cell DL SIR

- For a given RB, the received SIR at an FUE is

$$\text{SIR}_F = \frac{P_F \phi_F^{-1} H_F Q_F r_F^{-\alpha_F}}{P_M \phi_{FM}^{-1} H_{FM} Q_{FM} D_{FM}^{-\alpha_{FM}} + \sum_{i \in \Phi} P_F \phi_{FFi}^{-1} H_{FFi} Q_{FFi} D_{FFi}^{-\alpha_{FFi}}}$$

- $P_F = P_{F,Tx} G_{FAP} G_{UE}$ ,  $P_M = P_{M,Tx} G_{MBS} G_{UE}$ ;
- $D_{FM}$  is the distance from the MBS to the FUE,  $D_{FFi}$  is the distance from interfering FAP  $i$  to the FUE;
- $\alpha_F$ ,  $\alpha_{FM}$  and  $\alpha_{FFi}$  are path loss exponents from the home FAP, the MBS and an interfering FAP to the FUE, respectively;
- $H_F$ ,  $H_{FM}$  and  $H_{FFi}$  are unit-mean exponential channel power gains;
- $Q_F \sim \text{LN}(\zeta \mu_F, \zeta^2 \sigma_F^2)$ ,  $Q_{FM} \sim \text{LN}(\zeta \mu_{FM}, \zeta^2 \sigma_{FM}^2)$  and  $Q_{FFi} \sim \text{LN}(\zeta \mu_{FFi}, \zeta^2 \sigma_{FFi}^2)$  denote lognormal shadowing,  $\zeta = 0.1 \ln 10$ ;
- $\Phi$  is the set of FAPs transmitting in the given RB, with intensity  $u_F$ .

# Macrocell DL SIR

- Co-channel interference from neighboring macrocells is ignored.
- For a given RB, the received SIR at an MUE is

$$\text{SIR}_M = \frac{P_M \phi_M^{-1} H_M Q_M D_M^{-\alpha_M}}{\sum_{i \in \Phi} P_F \phi_{MF}^{-1} H_{MF_i} Q_{MF_i} D_{MF_i}^{-\alpha_{MF}}}$$

- $D_M$  is the distance from the MBS to the MUE,  $D_{MF_i}$  is the distance from FAP  $i$  to the MUE;
- $\alpha_M$  and  $\alpha_{MF}$  are path loss exponents from the MBS and an FAP to the MUE;
- $H_M$  and  $H_{MF_i}$  denote unit-mean exponential channel power gains;
- $Q_M \sim \text{LN}(\zeta\mu_M, \zeta^2\sigma_M^2)$  and  $Q_{MF_i} \sim \text{LN}(\zeta\mu_{MF}, \zeta^2\sigma_{MF}^2)$  denote lognormal shadowing.

# Femto Outage Probability

- Outage probability of an FUE w.r.t. the target SIR  $\gamma_F$

$$\begin{aligned} P(\text{SIR}_F < \gamma_F) &= P\left(\frac{S_F}{I_{\text{FM}} + \sum_{i \in \Phi} P_F \phi_{\text{FF}}^{-1} H_{\text{FF}i} Q_{\text{FF}i} D_{\text{FF}i}^{-\alpha_{\text{FF}}}} < \gamma_F\right) \\ &= P\left(\frac{S_F}{I_{\text{FM}}} < \gamma_F\right) + P\left(\text{SIR}_F < \gamma_F, \frac{S_F}{I_{\text{FM}}} \geq \gamma_F\right) \end{aligned}$$

- Based on the stochastic geometry theory and for an FUE at a distance  $d_{\text{FM}}$  from the MBS,

$$P(\text{SIR}_F < \gamma_F | D_{\text{FM}} = d_{\text{FM}}) \approx F_g\left(\frac{P_M \phi_F r_F^{\alpha_F} \gamma_F}{P_F \phi_{\text{FM}} d_{\text{FM}}^{\alpha_{\text{FM}}}}; \tilde{\mu}_F - \tilde{\mu}_{\text{FM}}, \sqrt{\tilde{\sigma}_F^2 + \tilde{\sigma}_{\text{FM}}^2}\right) +$$

$$\frac{\sum_{n=1}^N \sum_{m=1}^M w_n v_m \left\{ 1 - \exp\left[-\kappa_F u_F \left(e^{\sqrt{2a_n + 2\tilde{\chi}(b_m)} \tilde{\sigma}_F + \tilde{\mu}_F} - \gamma_F e^{\sqrt{2\tilde{\sigma}_{\text{FM}} b_m + \tilde{\mu}_{\text{FM}}}}\right)^{\frac{2}{\alpha_{\text{FF}}}}\right]\right\}}{2\pi \sqrt{a_n + \tilde{\chi}(b_m)} e^{\tilde{\chi}(b_m)}}$$

# Macro Outage Probability

- Outage probability of an MUE w.r.t. the target SIR  $\gamma_M$

$$P(\text{SIR}_M < \gamma_M) = P\left(\frac{S_M}{\sum_{i \in \Phi} P_F \phi_{MF}^{-1} H_{MF_i} Q_{MF_i} D_{MF_i}^{-\alpha_{MF}}} < \gamma_M\right)$$

- Based on the stochastic geometry theory and for an MUE at a distance  $d_M$  from the MBS,

$$P(\text{SIR}_M < \gamma_M | D_M = d_M) \approx 1 - \sum_{m=1}^M \frac{v_m}{\sqrt{\pi}} \exp\left[-\kappa_M u_F \exp\left(-\frac{2\sqrt{2}\tilde{\sigma}_M b_m}{\alpha_{MF}} - \frac{2\tilde{\mu}_M}{\alpha_{MF}}\right)\right]$$

$$\kappa_M = \pi \left(\frac{P_F \gamma_M}{\phi_{MF}}\right)^{\frac{2}{\alpha_{MF}}} \exp\left(\frac{2\tilde{\mu}_{MF}}{\alpha_{MF}} + \frac{2\tilde{\sigma}_{MF}^2}{\alpha_{MF}^2}\right)$$

# Minimum MBS-to-FAP Distance

- For an FUE at a distance  $d_{\text{FM}}$  from the MBS,

$$\begin{aligned} \mathbb{P}\left(\frac{S_{\text{F}}}{I_{\text{FM}}} < \gamma_{\text{F}} \mid D_{\text{FM}} = d_{\text{FM}}\right) &= \mathbb{P}\left(\frac{H_{\text{F}}Q_{\text{F}}}{H_{\text{FM}}Q_{\text{FM}}} < \frac{P_{\text{M}}\phi_{\text{F}}r_{\text{F}}^{\alpha_{\text{F}}}\gamma_{\text{F}}}{P_{\text{F}}\phi_{\text{FM}}d_{\text{FM}}^{\alpha_{\text{FM}}}}\right) \\ &\approx F_{\mathcal{G}}\left(\frac{P_{\text{M}}\phi_{\text{F}}r_{\text{F}}^{\alpha_{\text{F}}}\gamma_{\text{F}}}{P_{\text{F}}\phi_{\text{FM}}d_{\text{FM}}^{\alpha_{\text{FM}}}}; \tilde{\mu}_{\text{F}} - \tilde{\mu}_{\text{FM}}, \sqrt{\tilde{\sigma}_{\text{F}}^2 + \tilde{\sigma}_{\text{FM}}^2}\right) \end{aligned}$$

- $\mathcal{G} = H_{\text{F}}Q_{\text{F}}/(H_{\text{FM}}Q_{\text{FM}}) \sim \text{lognormal distribution}$

- Minimum  $d_{\text{FM}}$  for  $\mathbb{P}(S_{\text{F}}/I_{\text{FM}} < \gamma_{\text{F}} \mid D_{\text{FM}} = d_{\text{FM}}) \leq \varepsilon_{\text{F}}$ ,

$$d_{\text{FM},\text{min}} \approx \left[ \frac{P_{\text{F}}\phi_{\text{FM}}F_{\mathcal{G}}^{-1}\left(\varepsilon_{\text{F}}; \tilde{\mu}_{\text{F}} - \tilde{\mu}_{\text{FM}}, \sqrt{\tilde{\sigma}_{\text{F}}^2 + \tilde{\sigma}_{\text{FM}}^2}\right)}{P_{\text{M}}\phi_{\text{F}}r_{\text{F}}^{\alpha_{\text{F}}}\gamma_{\text{F}}} \right]^{-\frac{1}{\alpha_{\text{FM}}}}$$

- Any UE less than  $d_{\text{FM},\text{min}}$  from the MBS should be associated with the macrocell.

# Maximum Femto Density

- Maximum intensity of simultaneous co-channel femtocell transmissions at a distance  $d_M (\leq r_M)$  from the MBS for  $P(\text{SIR}_M < \gamma_M | D_M = d_M) \leq \varepsilon_M$

$$\tilde{u}_F(d_M) \stackrel{\Delta}{=} F_{\text{SIR}_M}^{-1}(\varepsilon_M, P_F, d_M)$$

$$F_{\text{SIR}_M}(u_F, P_F, d_M) = P(\text{SIR}_M < \gamma_M | D_M = d_M) = \varepsilon_M$$

- Maximum effective femtocell density at a distance  $d_{\text{FM}} (\geq d_{\text{FM},\text{min}})$  from the MBS for  $P(\text{SIR}_F < \gamma_F | D_{\text{FM}} = d_{\text{FM}}) \leq \varepsilon_F$

$$\tilde{u}_F(d_{\text{FM}}) \stackrel{\Delta}{=} F_{\text{SIR}_F}^{-1}(\varepsilon_F, P_F, d_{\text{FM}})$$

$$F_{\text{SIR}_F}(u_F, P_F, d_{\text{FM}}) = P(\text{SIR}_F < \gamma_F | D_{\text{FM}} = d_{\text{FM}}) = \varepsilon_F$$

- For  $d_{\text{FM},\text{min}} \leq d \leq r_M$ ,  $u_F(d) \leq \min\{\tilde{u}_F(d), \tilde{u}_F(d)\}$

# FAP Transmit Power

- Maximum allowed  $P_F$  at a distance  $d_M (\leq r_M)$  from the MBS s.t.  
 $P(\text{SIR}_M < \gamma_M | D_M = d_M) \leq \varepsilon_M$

$$\tilde{P}_F(d_M) \stackrel{\Delta}{=} F_{\text{SIR}_M}^{-1}(\varepsilon_M, u_F, d_M)$$

- Minimum required  $P_F$  at a distance  $d_{FM} (\geq d_{FM,\min})$  from the MBS  
s.t.  $P(\text{SIR}_F < \gamma_F | D_{FM} = d_{FM}) \leq \varepsilon_F$

$$\tilde{P}_F(d_{FM}) \stackrel{\Delta}{=} F_{\text{SIR}_F}^{-1}(\varepsilon_F, u_F, d_{FM})$$

- At a distance  $d$  ( $d_{FM,\min} \leq d \leq r_M$ ) from the MBS,
  - if  $\tilde{P}_F(d) \leq \check{P}_F(d)$ , then  $\tilde{P}_F(d) \leq P_F(d) \leq \check{P}_F(d)$ ;
  - otherwise, no femtocell coverage and have to reduce  $u_F = \lambda_F \rho$ .

# Simulations and Results

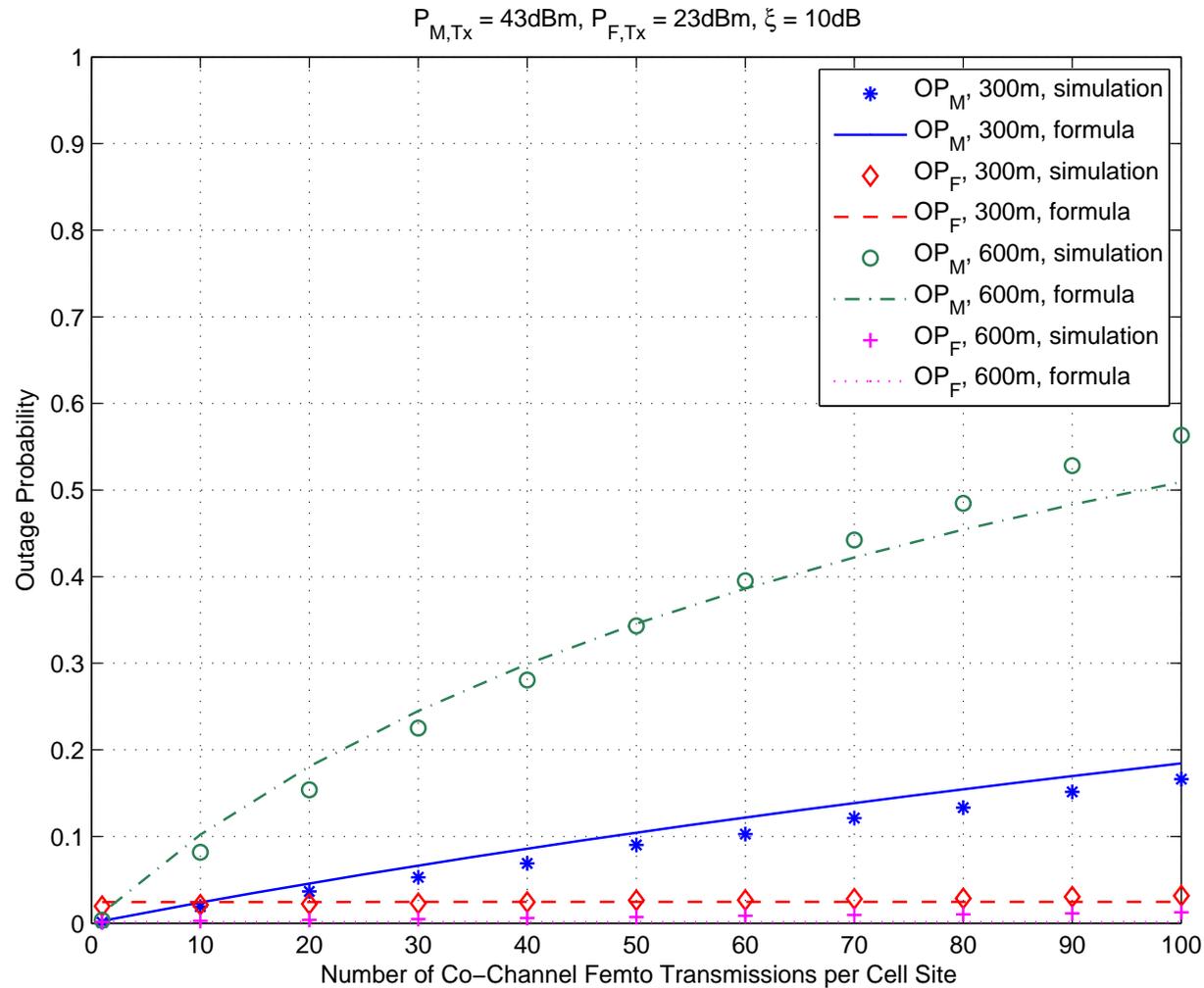


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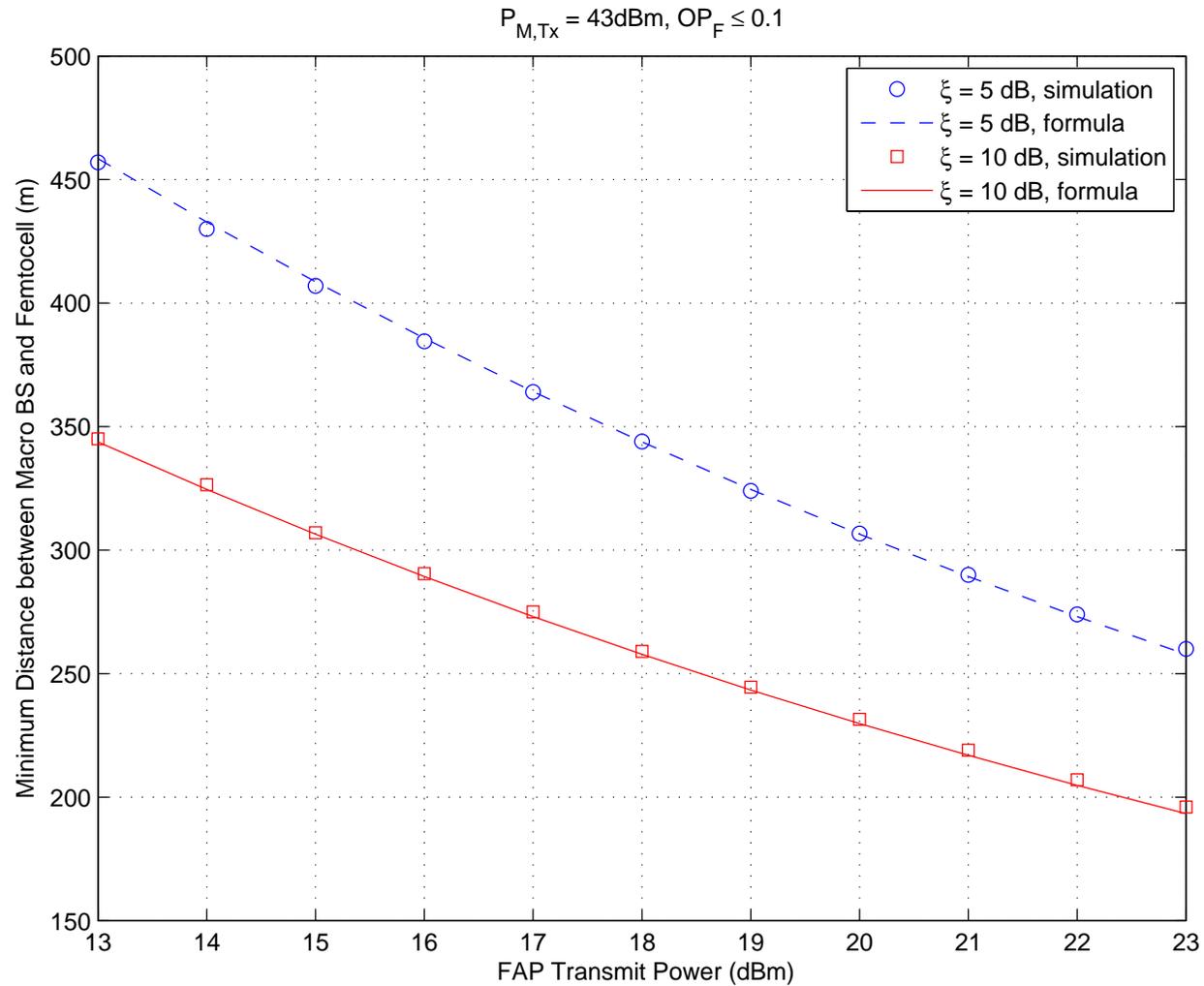
# Simulation Setup

- One MBS in the center
- FAPs and MUEs are randomly dropped within the macrocell coverage following independent SPPPs.
  - $\xi = 5$  dB, 10 dB
  - $\alpha_M = 4$
  - $\alpha_F = 3$
  - $\alpha_{FM} = \alpha_M$
  - $\alpha_{FF} = 3.5$
  - $\alpha_{MF} = \alpha_{FF}$
  - $\sigma_M = 8$  dB
  - $\sigma_F = 4$  dB
  - $\sigma_{FF} = 12$  dB
  - $\sigma_{MF} = 10$  dB
  - $\sigma_{FM} = 10$  dB
  - $f_c = 2000$  MHz
  - $P_{M,Tx} = 43$  dBm
  - $P_{F,Tx} \leq 23$  dBm
  - $G_{MBS} = 15$  dBi
  - $G_{FAP} = 2$  dBi
  - $G_{UE} = 0$  dBi
  - $r_M = 1000$  m
  - $r_F = 30$  m
  - $U_F = 2$
  - $\gamma_M = 3$  dB
  - $\gamma_F = 5$  dB
  - $\varepsilon_M = \varepsilon_F = 0.1$
  - $M = N = 12$

# Outage Probability

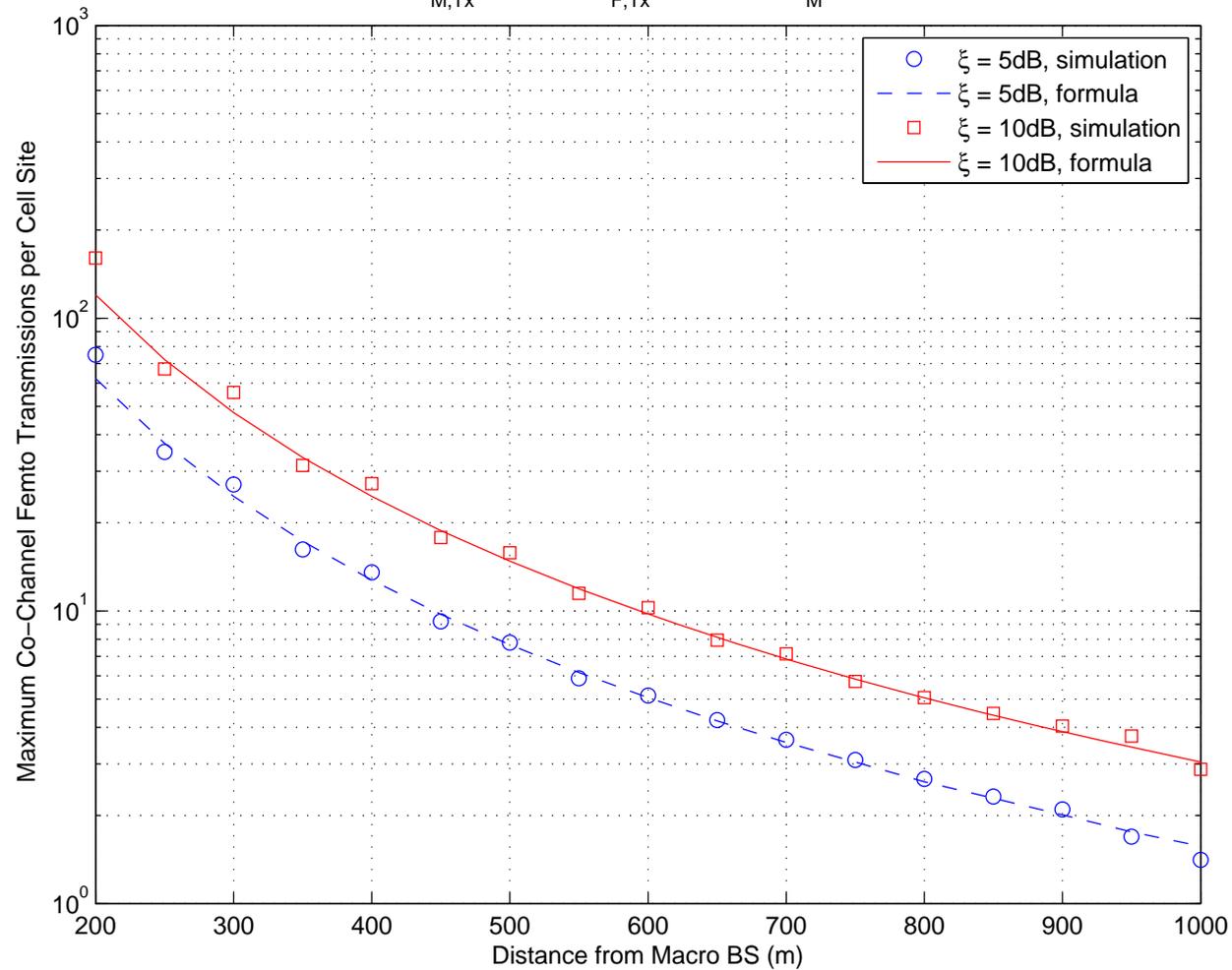


# Minimum MBS-to-FAP Distance



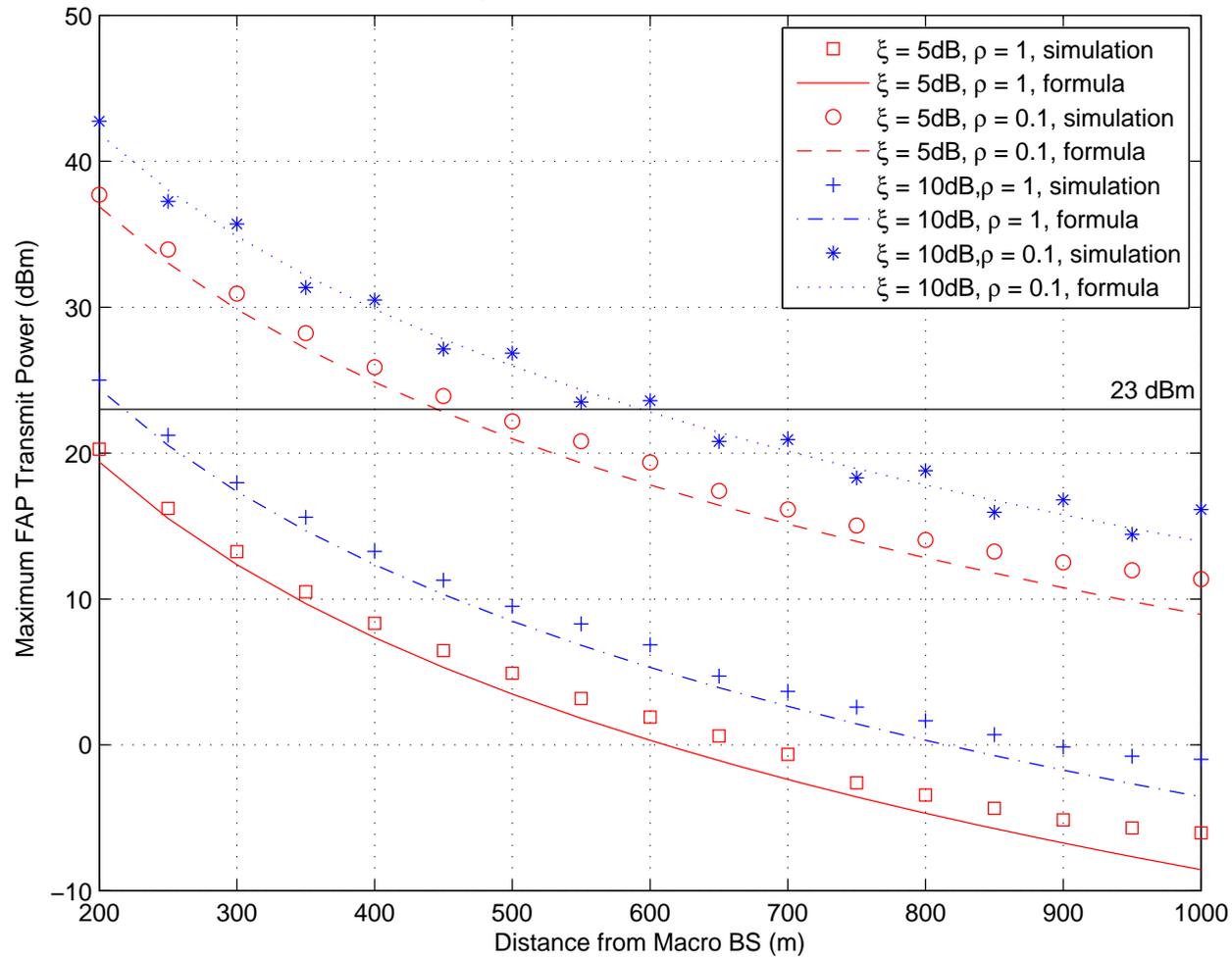
# Maximum Femto Density

$$P_{M,Tx} = 43\text{dBm}, P_{F,Tx} = 23\text{dBm}, OP_M \leq 0.1$$



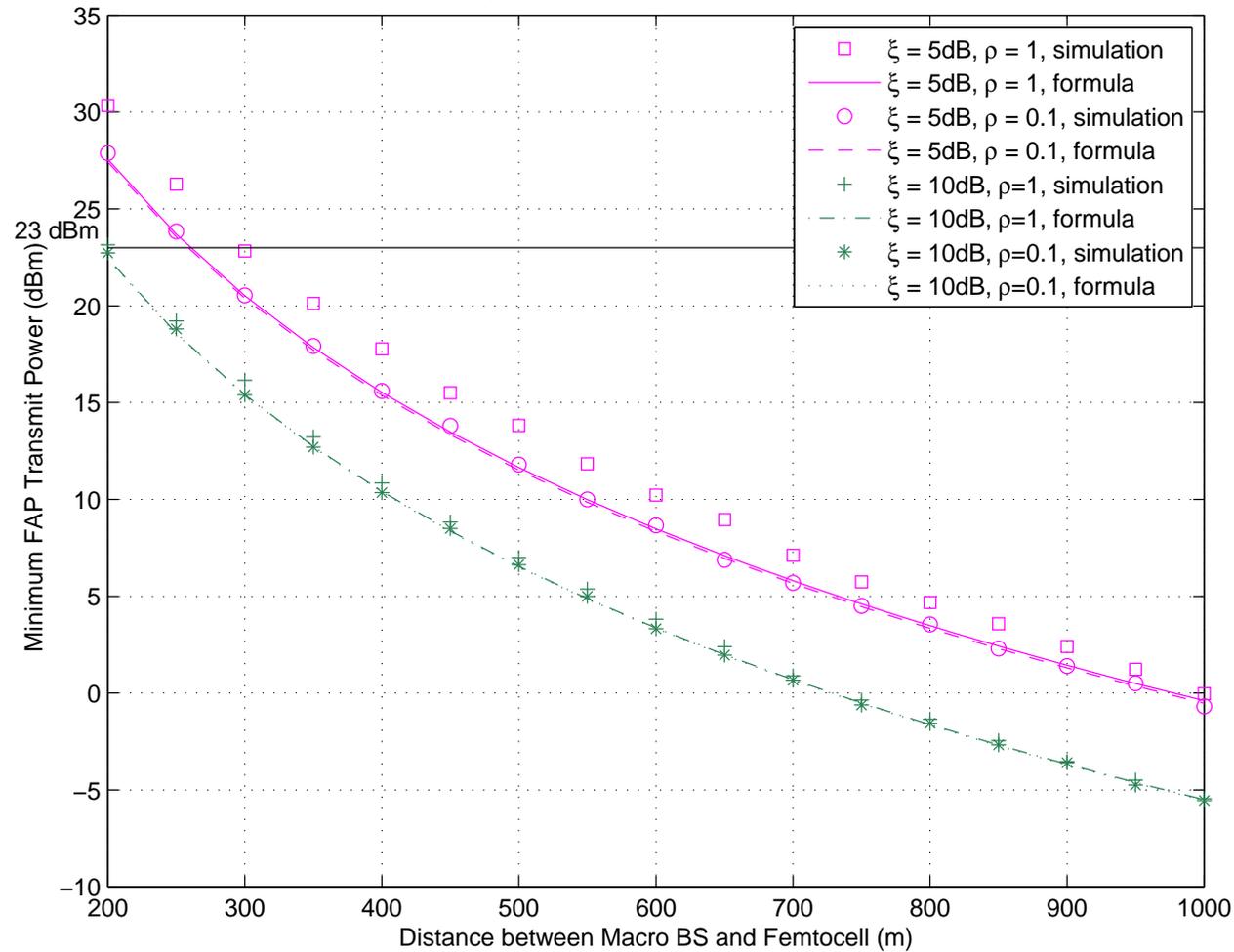
# Maximum Allowed $P_{F,Tx}$

$P_{M,Tx} = 43\text{dBm}, N_F = 100, OP_M \leq 0.1$



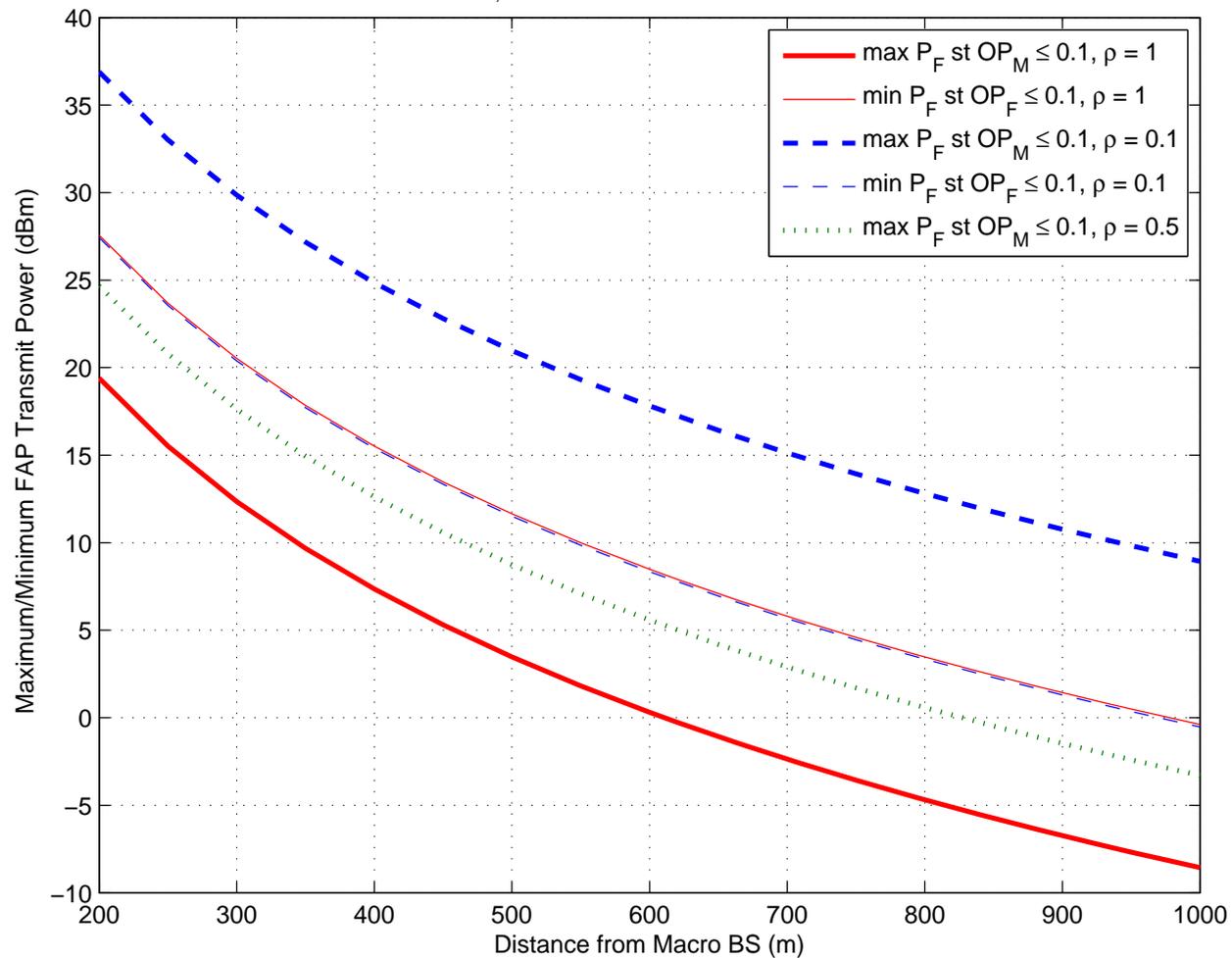
# Minimum Required $P_{F,Tx}$

$P_{M,Tx} = 43\text{dBm}$ ,  $N_F = 100$ ,  $OP_F \leq 0.1$



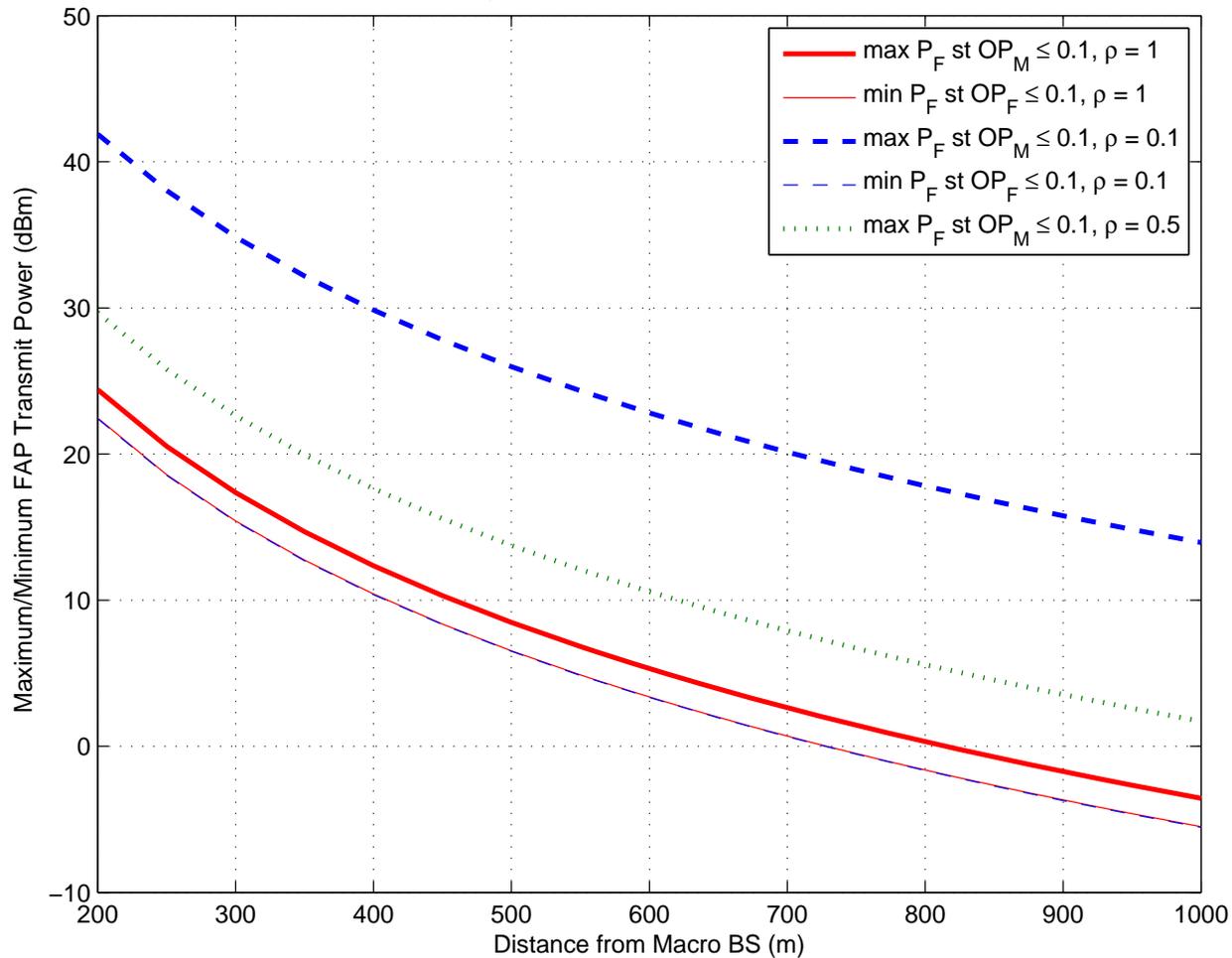
# $P_{F,Tx}$ under Low Attenuation

$P_{M,Tx} = 43\text{dBm}$ ,  $N_F = 100$ ,  $\xi = 5\text{dB}$



# $P_{F,Tx}$ under High Attenuation

$P_{M,Tx} = 43\text{dBm}, N_F = 100, \xi = 10\text{dB}$



# Conclusions

- OFDMA downlink of collocated spectrum-sharing macrocell and closed-access femtocells
  - Analytical expressions for outage probabilities
- It is possible to improve coverage by
  - regulating femtocell transmit powers, which depend on the distance from the MBS;
  - restricting the probability of each femtocell transmitting in each RB, which can be controlled in both frequency and time domains.

# Future Work

- Mechanism for an FAP to infer its distance from the closest MBS, so that the FAP can adapt its transmit power accordingly to ensure satisfactory coverage.
- Associate UEs to cells intelligently
  - UEs associated to a cell with least path loss
  - Allow more UEs to benefit from low-power BSs
- Distributed adaptive resource partitioning
  - BSs negotiate resource reservation with each other
  - Resource request/grant messages sent over backhaul
  - Based on load status and feedback from active UEs
- Coordinated multi-point transmission in the heterogeneous network



# Thank You !

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